

1 **HOW DOES MACHINE LEARNING COMPARE TO CONVENTIONAL**
2 **ECONOMETRICS FOR TRANSPORT DATA SETS? A TEST OF ML VS MLE**

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23 **ABSTRACT**

24
25 Machine learning (ML) is being used regularly in transportation and other applications to
26 predict response variables as a function of many inputs. This paper compares traditional
27 econometric methods of data analysis to ML methods in the prediction and understanding of
28 four key transport planning variables: household vehicle-miles traveled (a continuous
29 variable), household vehicle ownership (a count variable), mode choice (a categorical
30 variable), and land use change (a categorical variable with strong spatial interactions). Here,
31 the results of decision trees (DTs), random forests (RFs), Adaboost, gradient boosting
32 decision trees (GBDTs), XGBoost, lightGBM (gradient boosting methods), catboost, neural
33 networks (NNs), support vector methods (SVMs) and Naïve Bayesian networks (BN) are
34 compared to methods of ordinary least squares (OLS), multinomial logit (MNL), negative
35 binomial and spatial auto-regressive (SAR) MNL methods using the U.S.'s 2017 National
36 Household Travel Survey (NHTS 2017) and land use data sets from the Dallas-Ft. Worth
37 region of Texas. Results suggest that traditional econometric methods work pretty well on
38 the more continuous responses (VMT and vehicle ownership), but the RF, GBDT and
39 XGBoost methods delivered the best results, though the RF model required 30 to almost 60
40 times more computing time than XGBoost and GBDT methods. The RF, GBDT, XGBoost,
41 lightGBM and catboost offer better results than other methods for the two "classification"
42 cases (mode choice and land use change), with lightGBM being the most time-efficient.
43 Importantly, ML methods captured the plateauing effect that modelers may expect when
44 extrapolating covariate effects.

45 **Key words:** machine learning; artificial intelligence; econometric methods; travel behavior
46 prediction; model estimation comparisons; ensemble methods

47 **INTRODUCTION**

48 Machine learning (ML) is a branch of artificial intelligence (AI) that employs a variety of
49 statistical, probabilistic and optimization techniques. Instead of making strict assumptions

1 about random components and equations linking predictor variables or covariates to response
2 variables (X's to Y's), ML methods allow computers to “learn” and detect hard-to-discern
3 patterns from large, noisy and/or complex data sets. Thanks to computing advances, ML is
4 already being widely tested across various areas of transport data analysis, including truck-
5 type classification (Huang et al., 2018), mode recognition (Xie et al., 2003, Wang et al.,
6 2019), travel time prediction (Zhang et al., 2015), injury severity prediction (Delen et al.
7 2017, Hamad et al., 2019, Das et al., 2019), traffic flow prediction (Hosseini et al., 2019, Cui
8 et al., 2019), trip purpose identification (Deng et al., 2010), and automated-vehicle
9 applications (Liang et al., 2019). To date, the most commonly used ML algorithms appear to
10 be logistic regression (LR), using gradient ascent to calibrate model parameters (Caruana et
11 al., 2006; Chen et al., 2016; Delen et al., 2017), decision tree (DTs), the support vector
12 method (SVM), naïve Bayes (NB), k-nearest neighbors (KNN), K-means, random forest
13 (RF), bagging algorithms, gradient boosting decision trees (GBDT), XGBoost (extreme
14 gradient boosting), lightGBM (light gradient boosting method), and categorical boosting
15 algorithms (catboost). Some of these are old, traditional methods (based on basic clustering
16 math or a single sigmoidal equation). Others do not have target values or training data and are
17 used for smoothing behaviors with reinforcement along the way (e.g., a self-driving car
18 avoiding near-crashes and high centrifugal forces gets a higher score).

19 Data mining models have more flexible structures than traditional econometric models in
20 representing the relationship between the attributes of alternatives and choices. Thanks to
21 such flexibility, they may be able to offer valuable insights into relationships that random-
22 utility-based choice models cannot recognize (see, e.g., Xie et al., 2003, Xu et al., 2018, Keya
23 et al., 2019). Tree-based ML methods are often preferred by modelers because their
24 specifications are relatively clear (as a series of discrete branches, from variable to variable),
25 and this method appears to be quite resistant to outliers, noise/random errors, missing data,
26 and overfitting (using training data) (Harb et al., 2009). Compared to other ML methods,
27 which are regarded as black boxes, the tree-based ensemble methods (i.e., RF methods) are
28 easily interpreted and can solve complex nonlinear relationship, which enable a better
29 understanding of Y-vs-X relationships (Zhang et al., 2015). The following will describe the
30 ensemble methods from Bagging to Boosting.

31 *Bagging*

32 RF is a common bagging methods that combines Brieman's bagging idea with Ho's random
33 subspace method (Harb et al., 2009). Cheng et al. (2019) and Seksar et al. (2014) reviewed
34 many recent RF studies, finding consistently strong predictive accuracy across distinctive
35 data sets. RF also can identify, interpret, and rank-order the relevance of competing
36 covariates and their interactions. Bagging methods involves random sampling of small
37 subsets of data, and gives all resulting weak models equal probability. So each sample and its
38 associated model have the same weight, running in parallel, which is very different from
39 boosting methods, since those give more weight or credit to stronger/less weak models
40 among the samples.

41 *Boosting*

42 Freund (1997) proved that using “boosting” algorithms to combine many weak models can
43 result in a single and highly accurate model - one of the most powerful ideas for prediction
44 over the past 20 years (Hou et al., 2018). Boosting methods use the same data set to run the
45 prediction models, with the same weight given to each data set when predicting the first weak
46 model, then using prediction error rates to adjust sample and model weights to predict the
47 next model combination. Thus, boosting methods must run in sequence, which slows
48 prediction speeds but delivers better prediction accuracy, as compared to bagging methods
49 (Caruana et al., 2006). Gradient boosting, which combines gradient descent and boosting to
50 improve prediction speed and accuracy, is an extension of the over-boosting method

1 (developed by Friedman [2001]). Such algorithms are typically one of the following four
2 methods: GBM (gradient boosting method), XGBoost, lightGBM, and catboost.

3 GBMs generate base models sequentially and improve prediction accuracy since
4 misclassified or incorrectly estimated samples are more likely to be selected (using larger
5 weights) on successive estimation rounds. Zhang et al. (2015) used a gradient boosting
6 regression tree (a kind of GBM) to predict travel times with greater accuracy than ARIMA
7 and RF. Ding et al. (2016) devised the GBDT method (a kind of GBM) to estimate short-term
8 subway ridership levels (by station) and showed how GBDT can reliably rank the relative
9 influence of different covariates - like bus transfer activities and temporal features (Time of
10 day, day, week and month were incorporated in the prediction model). It is also used
11 compared to BP-NN, SVM and RF. For BP-neural network, and found that GBDT model
12 receives the best model performance (higher R^2). Proposed by Freund in 1997, Adaboost is
13 another kind of GBM to compare to RF (Miao et al., 2010), NN (Alfaro et al., 2008), and
14 SVM (Wang et al., 2006). All of the results showed that AdaBoost outperforms other
15 methods and is more robust than SVM.

16 Recently, XGBoost has received a lot of attention. Hou et al. (2018) used single DT, RF,
17 GBM and XGBoost to predict roadway traffic flows and found similar accuracy across
18 methods, with XGBoost requiring the lowest computing times. Wang (2018) used the
19 XGBoost, lightGBM and DTs methods to predict travel mode choices and found the
20 lightGBM and XGBoost methods be more accurate than DTs, with lightGBM most preferred.

21 Compared to GBDT, Ke et al. (2017) verified that lightGBM reduced training times by 95%
22 or more, while achieving nearly the same predictive accuracy (measured as AUC). The main
23 difference between lightGBM and the XGboost algorithms is that lightGBM uses a
24 histogram-based algorithm to speed up the training process, reduce memory consumption,
25 and adopt a leaf-wise leaf-growth strategy with depth limitations (Guo et al., 2017). Catboost
26 is also a cutting-edge ML technique, which is good at dealing with categorical data.
27 (Dorogush et al. 2018).

28 As analysis before, ensemble methods generally deliver better predictions than other
29 algorithms. Consider ANN, SVM and Bayesian network models are also widely used in
30 model prediction. This paper tested the following 10 ML models: decision trees (DTs),
31 random forests (RFs), Adaboost, gradient boosting decision trees (GBDT), XGBoost,
32 lightGBM, catboost, ANNs, SVMs and Bayesian networks. All these methods can be used
33 for categorical or count or continuous response variable prediction. Their results were then
34 compared to those from traditional estimation models (OLS, negative binomial, and MNL
35 specifications) for prediction of annual household VMT, household vehicle ownership, and
36 mode choices. Spatial econometric techniques (MNL SAR) were also used to analyze the
37 land use change data. Data come from Dallas-Ft. Worth's 2017 National Household Travel
38 Survey (NHTS 2017) add-on sample and from the Dallas-Ft. Worth region more generally
39 (via its metropolitan planning organization: the North Central Texas Council of
40 Governments, or NCTCOG).

41 Interestingly, almost no ML users in the world are yet making their ML model specifications
42 transparent. For example, Hou et al. (2018), Linero and Nethery (2015), Folden (2018), Goh
43 (2018), Brown (2019), Pu (2019), and nearly all others only compare competing models'
44 predictive accuracy (using, e.g., root-mean-squared errors [RMSE values]) and simply rank
45 the explanatory variables (on the basis of $dE(y)/dx$ slope comparisons, typically). Thus, this
46 new paper examines not just goodness of fit in predicting hold-out sample values, but
47 emphasizes interpretation of results for behavioral understanding, smarter planning and
48 policy making, and better investment and management decisions.

49 MACHINE LEARNING (ML) METHODS

1 ML methods are extensive. Because ANNs, BN and SVM are three common methods which
2 are already used before the ML and AI emerge, and many papers have describe these three
3 algorithms, meanwhile, due to space constraints, more information on ANNs, BN and SVM
4 methods can be found in Xiao et al. (2015), Omrani (2015), Delen et al. (2017) and Iranitalab
5 (2017). This paper will pay more attention to ensemble methods, below are key details for
6 specifications of Bagging and Boosting.

7 ***Bagging Trees via Random Forest***

8 Breiman proposed the RF method in 1996. RFs combine decision tree (DT) predictors by
9 using bootstrap method, and then using voting (for classifier) or average (for regression) the
10 results of each DT to obtain the final prediction value. In RF, each decision node uses the
11 best among a subset of predictors randomly chosen at that node. This method has performed
12 very well compared to many other commonly-used classifiers and is resistant to overfitting
13 (Breiman, 1996).

14 ***Boosting Techniques***

15 This section describes 5 top boosting methods: Adaboost, GBDT, XGBoost, lightGBM and
16 catboost, which are presented in the chronological order they were introduced in the
17 literature, also from simpler to more complex.

18 ***Adaboost***

19 Adaptive boosting (Adaboost) was introduced by Freund and Shapire in 1997; it combines a
20 collection of weak models to provide a stronger model. With m training-set data points, this
21 method uses initial weights of $1/m$ for each observation to “train” (i.e., estimate) a set of base
22 (initial, weak) models. The predictions of these (the number of base models depend on the
23 prediction accuracy and overfitting or not) base models are used to generate a new set of
24 weights call α values by using prediction accuracy ($\alpha = 0.5 * \ln(1 - accuracy/total) /$
25 ($accuracy/total$)), which are then used to update data-point weights. Larger weights are
26 assigned to samples with more misclassified data points (i.e., to harder-to-predict data sets),
27 and these updated weights are used to train the next model version. Final predictions for each
28 data point are obtained as an α -weighted “voting” (or score) total across all upstream
29 models (Krishnaveni et al., 2011).

30 ***Gradient Boosting Decision Tree (GBDT)***

31 Like other boosting methods, GBDT combines several relatively weak models into a stronger
32 model. It uses forward stage-wise additive modeling, GBDT only can uses CART
33 (Classification And Regression Tree, which use Gini impurity to select the node classifier
34 variables, smaller Gini impurity means better prediction accuracy) trees to be the base
35 learners, loss of function is minimized in the direction of its steepest-descent, the aim of each
36 iteration is to decrease the last residual. GBDT algorithms resist noise components and outlier
37 data points by bagging and adding regularization, making GBDT more robust than other
38 methods. For these reasons, GBDT is now widely used for classification of data points,
39 prediction of continuous response variables (which ML users call “regression”), and ranking
40 of outcomes or decisions (Ding et al., 2016).

41 ***Extreme Gradient Boosting Model (XGBoost)***

42 Friedman (2001) proposed the XGBoost model as a well-developed algorithm in the boosted
43 DT family (Hou et al., 2018). It also is trained (estimated) in a forward “stage-wise” (i.e.,
44 input by input) fashion, to minimize the “loss function” (typically the sum of squared error
45 terms), by adjusting parameters bit by bit (to remove residual correlation between an input
46 variable and the loss function). XGBoost uses a parallel tree boosting method (also known as
47 GBM with DTs) that solves many data science problems in a fast and accurate way (Hou et
48 al., 2018). It can use CART or gblinear as its base model, and add regulation to the objective

1 function. A second-order Taylor series expansion is used to approximate the method's
2 objective function (i.e., its loss function, like the RMSE), based on second derivatives.

3 ***LightGBM***

4 For very large data sets, the LightGBM technique is often helpful. It combines gradient-based
5 one-side sampling (GOSS) and exclusive feature (covariate) bundling (EFB) to tackle the
6 problem of model complexity (thanks to a very large set of covariates and/or training data).
7 GOSS method keeps those instances with large gradients, and only randomly drop those
8 instances with small gradients (leaf-wise tree growth strategy with depth limited [other
9 algorithms grow level-wise]). LightGBM has been found to accelerate “training speed” (i.e.,
10 estimation times) while delivering accuracy compared to other ML methods (Ke et al., 2017).

11 ***Catboost***

12 The Yandex Company proposed “Catboost” in 2017 to boost estimation for categorical data.
13 Catboost is considered a cutting-edge ML technique, able to compete with any leading ML
14 algorithm on the performance front (Dorogush et al. 2018). Catboost, which use complete
15 binary tree, can be used without any explicit pre-processing of input values to convert
16 categories into numbers, so it can handle categorical “features” (i.e., covariates)
17 automatically. More specifically, data set is randomly permuted firstly, then for each
18 sample, it calculates average label value for samples with the same category value prior to the
19 given one in the permutation, which is different from one-hot encoding. It also reduces the
20 need for extensive parameter tuning and lowers the chances of overfitting, which leads to
21 more robust prediction (Dorogush et al., 2018).

22 **MODEL FIT ASSESSMENT**

23 Different model-fit statistics or loss-function values are used to evaluate and compare ML
24 and other estimation techniques. The better score statistic to use generally depends on the
25 response variable's characteristics (e.g., is it binary, categorical, ordered or continuous?). The
26 following sections discuss scoring techniques, starting with a classification case.

27 ***Classification Problems for Categorical Response Data***

28 Contents of a confusion matrix for response categorization are commonly used to compare
29 competing models' performance, based on the metrics of recall, precision, F_1 score, and what
30 ML modelers call “AUC” (which stands for area under the receiver operating characteristic
31 or ROC curve).

33 Using a 3-category example, class or category i 's precision is simply the fraction of data
34 points categorized correctly into class i : $p_i = n_{ii} / (n_{ii} + n_{i2} + n_{i3})$, where n_{ij} is the number of data
35 points with a class i response that are model-classified as class j .

36 The 3 positive predictive values (p_1 , p_2 and p_3) and the true positive rates of the three classes
37 ($P_1 = n_{11}/n_{i1}$, $P_2 = n_{22}/n_{i2}$, and $P_3 = n_{33}/n_{i3}$) are then harmonically averaged to calculate the
38 index called F_{1score} , which is $1/3(\sum(1/p_i + 1/P_i))$, and this statistic ranges from 0 to 1, with 1
39 being the best score feasible (with all class 1 data points properly categorized, and no others
40 mistakenly placed in that category).

41 ***Regression Problem (Continuous Response Variable Prediction)***

42 Scoring criteria commonly used to improve models and compare models with continuous
43 response variables are the mean square error (MSE), mean absolute error (MAE), root mean
44 square error (RMSE), root mean squared logarithmic error (RMSLE), and coefficient of
45 determination (R^2) or correlation between actual and predict values ($\rho = \text{sqrt}(R^2)$ in the
46 bivariate context). The R^2 and RMSE values are defined in Eqs. 2 and 3:

$$47 \quad RMSE = \sqrt{\frac{1}{n} \sum (y_i - \hat{y}_i)^2} \quad (2)$$

$$R^2 = 1 - \frac{\sum((y_i - \hat{y}_i)^2)}{\sum((y_i - \bar{y})^2)} \quad (3)$$

where y_i is the observed output value, and \hat{y}_i is the model-predicted response or output.

Avoiding Overfitting

ML results can suffer from overfitting problems, since they can have hundreds, thousands or more parameters embedded in them, making them too responsive to outliers and demanding very large data sets, which many researchers will not have. ML researchers avoid this issue by holding out a testing (validation) sample of the data, apart from the training (calibration) data set used to create the model. Using random processes, if there a considerable deviation in model prediction accuracy between these two distinctive data sets, parameters in the trained model are adjusted. ML routines are typically programmed to replicate this process of partitioning the initial data set, fitting the model (on each training data set), and evaluating the success rate or scores R different times. The average of these scores is the overall success rate.

Sensitivity

Many people feel that ML methods are like black boxes, since few make explicit the parameters and equations behind them, or at least the relationships between outputs and inputs (i.e., between response values Y and each explanatory variable X_i). New sensitivity analyses have been proposed to address this long-standing weakness (Delen et al., 2017). In this paper, the average change in model-predicted output values (ΔY) with respect to a 1 standard deviation or binary (0 to 1) change in every input (for every data point) is used to appreciate the relationship between each explanatory variable and the dependent variable. This effect is calculated differently for continuous versus binary inputs (e.g., $x_1 = \text{Age}$ vs $x_2 = \text{Gender}$ or $\text{Presence of Children in the Respondent's Household}$), since the latter does not change smoothly/continuously in practice. The difference in the average response was divided by the response variable's standard deviation to normalize the impacts, for ready comparison across different response-variable contexts (e.g., $Y_1 = \text{VMT}$ vs. $Y_2 = \text{Vehicle Ownership}$). As shown in Eq. 4.

$$\Delta Y \text{ w.r. t } = \frac{y_{\text{changed}} - y_{\text{unchanged}}}{\sigma} \quad (4)$$

DATA SETS

This work relies on two data sets to do estimate four distinctive response variables. These are the Dallas-Ft. Worth or “DFW” sample in the U.S. 2017 National Household Travel Survey (NHTS 2017) data set and the land use data sets provided by DFW’s metropolitan planning organization (NCTCOG). After removal of records with missing covariates, the four data sets’ sample sizes are as follows: daily household-level VMT: $n_1 = 8,676$ households; vehicle ownership: $n_2 = 8,545$ households; model choice: $n_3 = 13,834$ person-trips; and land use change: $n_4 = 99,304$ grid cells (each measuring 30 m by 30 m).

The data sets contain a variety of valuable variables, including individual and household demographics, trip-level and mode-alternative attributes and neighborhood land use and access details. Table 1 provides summary statistics for all variables considered here.

TABLE 1 Summary Statistics for four Transportation-related Data Sets

HHVMT Model ($n_1 = 8,676$)					
Variable	Description	Mean	Std. Dev.	Min	Max
HHVMT	Vehicle-miles travelled (miles)	25,612.44	21,823.6	2	402,000
Own Home	1. Own (76.40%); 2. Rent (23.60%)	1.236	0.425	1	2
HH Size	# household members	2.229	1.202	1	10
#HH Veh	# household vehicles	1.971	1.0515	0	10

HH Income	Household income per year	\$85,517	\$56,975	\$5,000	\$202,000
#Drivers	# household drivers	1.744	0.753	0	7
#HH Trips	# person-trips on travel day	7.463	5.947	0	53
#Children	# of children in household	0.105	0.384	0	4
#Workers	# household workers	1.141	0.881	0	5
UrbRur	1. Urban (92.37%); 2. Rural (7.63%)	--	--	1	2
DistCBD	Distance to the CBD (miles)	22.67	12.34	0.119	73.82
Workerden	Workers per square mile in the census tract of the household's home location	1,892.5	1,393.7	25	5,000
Vehicle Ownership Model (n₂ = 8,545)					
Variable	Description	Mean	Std. Dev.	Min	Max
#HH Veh	Count of household vehicles	1.974	1.054	0	10
Own Home	1. Own (74.37%); 2. Rent (25.63%)	--	--	1	2
HH Size	Count of household members	2.234	1.206	1	10
HH Income	Household income	\$86,245.47	\$58,442.45	\$5,000	\$210,000
#Drivers	Count of household driver	1.746	0.754	0	7
#Workers	Count of household worker	1.144	0.881	0	5
UrbRur	1. Urban (92.29%); 2. Rural (7.71%)	1.077	0.267	1	2
Popden	Population density (persons per square mile) in the census tract of the household's home location.	3,673.54	3,189.55	5,619	41,300.6
Mode Choice Model (n₃ = 13,834)					
Variable	Description	Mean	Std. Dev.	Min	Max
Mode Choice	1. Drivealone (52.33%); 2. Carpool (39.94%); 3. Walk/Bike (3.85%); 4. Transit (3.87%)	--	--	--	--
Travel Time	Travel time (min)	53.615	63.018	1	1,160
Cost	Cost	\$4.56	\$18.77	\$0	\$654.78
Trip Purp	3 Trip purposes: 1. NHB (21.62%); 2. HBO (51.77%); 3. HBW (26.6%) = Non-home based, home-based other/non-work, and home-based work trips	--	--	1	3
Age	Age of the traveler	45	21	5	100
Driver	1. Yes (83.02%); 2. No (16.97%)	1.1697	0.3754	1	2
Sex	1. Male (47.46%); 2. Female (52.53%)	1.5253	0.4993	1	2
HH Size	Count of household members	2.8361	1.3882	1	10
#HH Veh	Household vehicle number	2.235	1.0582	0	10
HH Income	Household income	98,871	66,483	5,000	250,000
Workerden	Workers per square mile in the census tract of household's home location.	1,806.9	1,694.6	9.25	19,269.2
Land Use Change Model (n₄ = 99,304)					
Variable	Description	Mean	Std. Dev.	Min	Max
Land use change	1. Residential (6.69%); 2. Commercial/civic (2.00%); 3. Underdeveloped (60.90%); 4. Other (6.21%); 5. Ranch land (24.20%).	--	--	--	--
Builtdens_SF_1mi	Pixel density per square mile within 1 mile of all single-family pixels built as of 2010.	276.757	335.7188	0	2170.5
Chgdens_MF_2mi	Pixel density per square mile within 2 miles of all multi-family pixels built between 1990 and 2010.	22.61893	37.74299	0	468.38

Chgdens_com_3mi	Pixel density per square mile within 3 miles of all commercial pixels built between 1990 and 2010.	29.696	41.116	0	405.82
Chgdens_2mi	Pixel density per square mile within 2 miles of all pixels built between 1990 and 2010.	253.630	236.559	0	1416.3
Disemp	Distance to an "employment cluster" zip code in 2010.	27451.25	17072.42	0	66798
Empdens_3mi	Density of all jobs located within 3 miles in 2010.	266.607	791.504	0	14033
Elevation	Elevation in feet above mean sea level.	754.799	193.668	340.01	1357.8

1 Notes: 1 pixel = 30 m * 30 m (approx. 0.25 acres). Only 3.7% of all pixels were used, due to excessively large
2 data set size being transferred to the research team, for this very large metroplex region. These are uniformly
3 sampled in space, so their centroids are 150 meters apart in a grid across the region, to give wide dispersion in
4 land use settings.

5 *Experiments*

6 Each of the four data sets were randomly split into two sets (70% for training and 30% for
7 testing) ten times, with results averaged over the 10 different estimation runs for each of the
8 ML methods deemed most competitive for the different response variables. Python codes
9 from the scikit-learn were used in this paper to run the ML methods, lightGBM and catboost
10 packages were installed in Python, and Stata was used to run the MLE model.

11 **RESULTS**

12 Tables 2 and 3 summarize model results in terms of computing time, predictive accuracy
13 (using R^2 values), and RMSE or recall and F_1 scores (depending on type of response variable
14 being estimated). Carrion-Flores' (2009) multinomial logit model with spatial auto-regression
15 (MNL-SAR) specification was used to predict the land use changes across much of the DFW
16 region (11 counties) between 2010 and 2015. For the regression models, The GBDT and RF
17 achieve a better prediction accuracy, while RF takes longer running time than the GBDT. In
18 the classification models, the catboost, GBDT, XGboost and lightGBM achieve better
19 prediction accuracy, while the running time of lightGBM being the most time-efficient.

20

21 **TABLE 2 Regression Model Comparisons based on Computing Time, Predictive**
22 **Accuracy, R^2 and RMSE (for HH VMT& HH Vehicle Ownership)**

Method Used	Run Time (seconds)	Training Accuracy (R^2)	Test Data Set Accuracy (R^2)	RMSE
Annual HHVMT Prediction Results using OLS vs. ML Methods				
OLS	0.14	0.479	0.468	15754.88
Decision Tree (DT)	0.07	0.526	0.431	14534.29
Random Forest (RF)	49.49	0.594	0.497	11433.93
AdaBoost	17.48	0.382	0.323	17318.64
GBDT	3.56	0.642	0.542	9589.14
XGBoost	0.98	0.569	0.488	11867.06
lightGBM	4.49	0.512	0.452	12885
NN	9.56	-0.0123	-0.0359	21567.33
SVM	5.48	-0.06603	-0.0666	22043.15
HH Vehicle Ownership Prediction Results using Negative Binomial vs. ML Methods				
Poisson regression	0.169	0.4526	0.4319	0.779
Decision Tree (DT)	0.03	0.5372	0.5029	0.699
Random Forest (RF)	18.28	0.5786	0.5251	0.639
AdaBoost	1.82	0.5138	0.4804	0.729
GBDT	0.61	0.5855	0.5246	0.645

XGBoost	0.68	0.5618	0.492	0.680
LightGBM	0.26	0.539	0.4924	0.683
SVM	0.56	-0.2536	-0.1322	1.121
NN	2.52	-0.7005	-0.6547	1.131

1

2 **TABLE 3 Computing Time, Training Accuracy, Precision, Recall and F₁score Values for**
3 **Mode Choice & Land Use Change Prediction**

Method Used	Time (seconds)	Training accuracy	Precision	Recall	F ₁ score
Mode Choice Prediction Results by MNL and ML					
MNL	0.83	0.658	0.63	0.64	0.63
Decision tree	0.09	0.976	0.98	0.98	0.98
Random Forest (RF)	13.24	0.989	0.98	0.98	0.98
AdaBoost	0.24	0.877	0.81	0.88	0.84
XGBoost	6.15	0.989	0.99	0.99	0.99
GBDT	7.00	0.994	0.99	0.99	0.99
NN	0.71	0.556	0.65	0.56	0.60
NBayes	0.06	0.856	0.85	0.86	0.84
catboost	60.63	0.993	0.99	0.99	0.99
lightGBM	2.20	0.997	0.99	0.99	0.99
Land Use Change Prediction Results by MNL SAR and ML					
MNL SAR	8.93	0.643	0.64	0.64	0.64
Decision Tree (DT)	1.04	0.714	0.67	0.70	0.68
Random Forest (RF)	30.97	0.744	0.72	0.71	0.71
AdaBoost	29.24	0.612	0.53	0.61	0.57
Extra trees	49.27	0.65	0.66	0.65	0.65
XGBoost	143.82	0.76	0.74	0.73	0.73
GBDT	208.82	0.769	0.73	0.74	0.73
NN	256.56	0.626	0.55	0.63	0.59
NBayes	0.32	0.348	0.47	0.34	0.39
catboost	161	0.743	0.74	0.74	0.74
lightGBM	19.34	0.733	0.73	0.72	0.72

4 Notes: Extra trees is a variation of RF model, it is tested and shows prediction accuracy worse than RF.

12 In terms of **HHVMT** prediction, the GBDT proved most effective relative to the many other
13 models examines, achieving highest prediction accuracy in just 3.56 seconds, followed by the
14 random forest technique, which took 49.5 sec, (almost 14 times longer), but is considered a
15 more transparent model (with interpretable branches across all input variables used)

16 In terms of **HH vehicle ownership** prediction, the GBDT and RF methods outperformed the
17 other models (with the RF requiring 30 times more computing time than the GBDT). RF's
18 performance was followed by a simple, single DT.

19 In terms of **mode choice** prediction, the DT and ensemble methods beat the MNL approach,
20 while catboost required much longer running times than XGBoost, GBDT and lightGBM.

21 For **land use change** predictions (over the 20-year data period), the catboost method
22 achieved the highest F₁score (of 0.74), which is only slightly higher than that of the XGBoost
23 (0.73), GBDT (0.73), lightGBM (0.72) and RF (0.71) methods. This required only slightly
24 (11%) more run time than XGBoost required, 8.32 times more than lightGBM, and 5.2 more
25 than RF, but 77% less computing time than GBDT. So lightGBM may be best used in

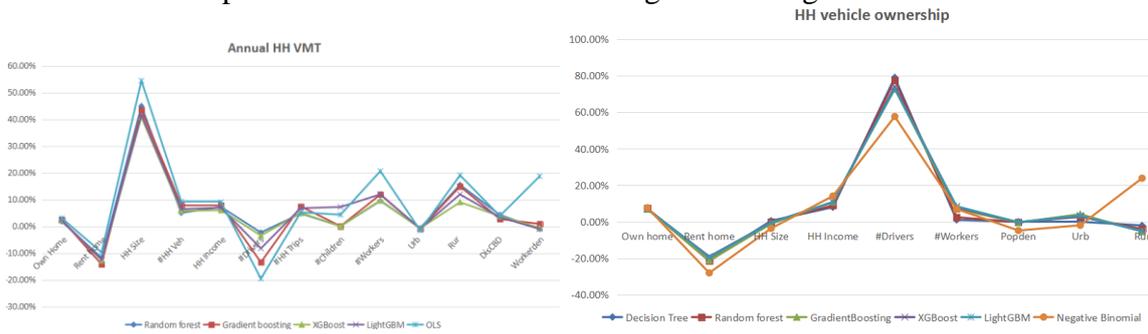
1 predicting land use changes, if run times are a concern (which will depend on application
 2 needs and data set size).

3 **Estimates of Practical Significance across Competing Models**

4 Using Eq. 4, estimates of the practical significance of input variables for each of the four
 5 output variables can be calculated. Here, only the top ML models' estimates are compared to
 6 those from the traditional econometric methods used, and just for a few of the input variables,
 7 to illustrate differences, while respecting word-count constraints.

8 Practical significance is imputed by increasing each input value for each data point in each
 9 data set. For example, inputs of HHsize and #Workers were varied from 1 to 6 to appreciate
 10 each model's estimate of how this would impact a household's expected VMT.

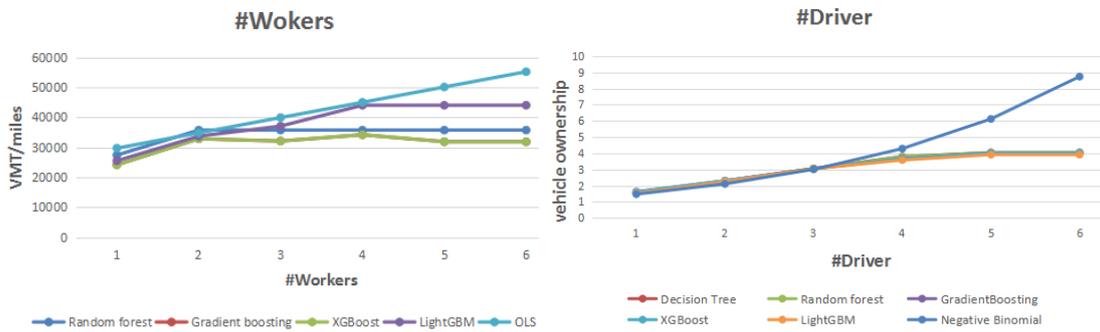
11 The prediction results comparison for the four models and practical significance analysis
 12 results for some important variables are shown in Figure 1 through 3.



13

14 (a) Influence of Variables on VMT

(b) Influence of Variables on HH Vehicle Ownership

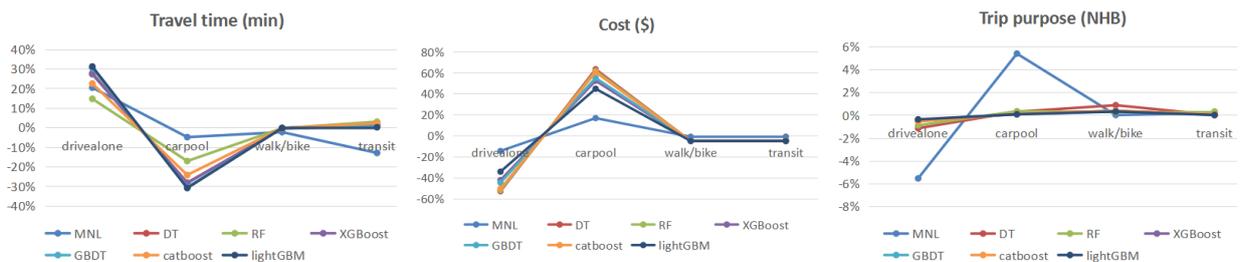


15

16 (c) Influence of Number of Workers Increase on VMT

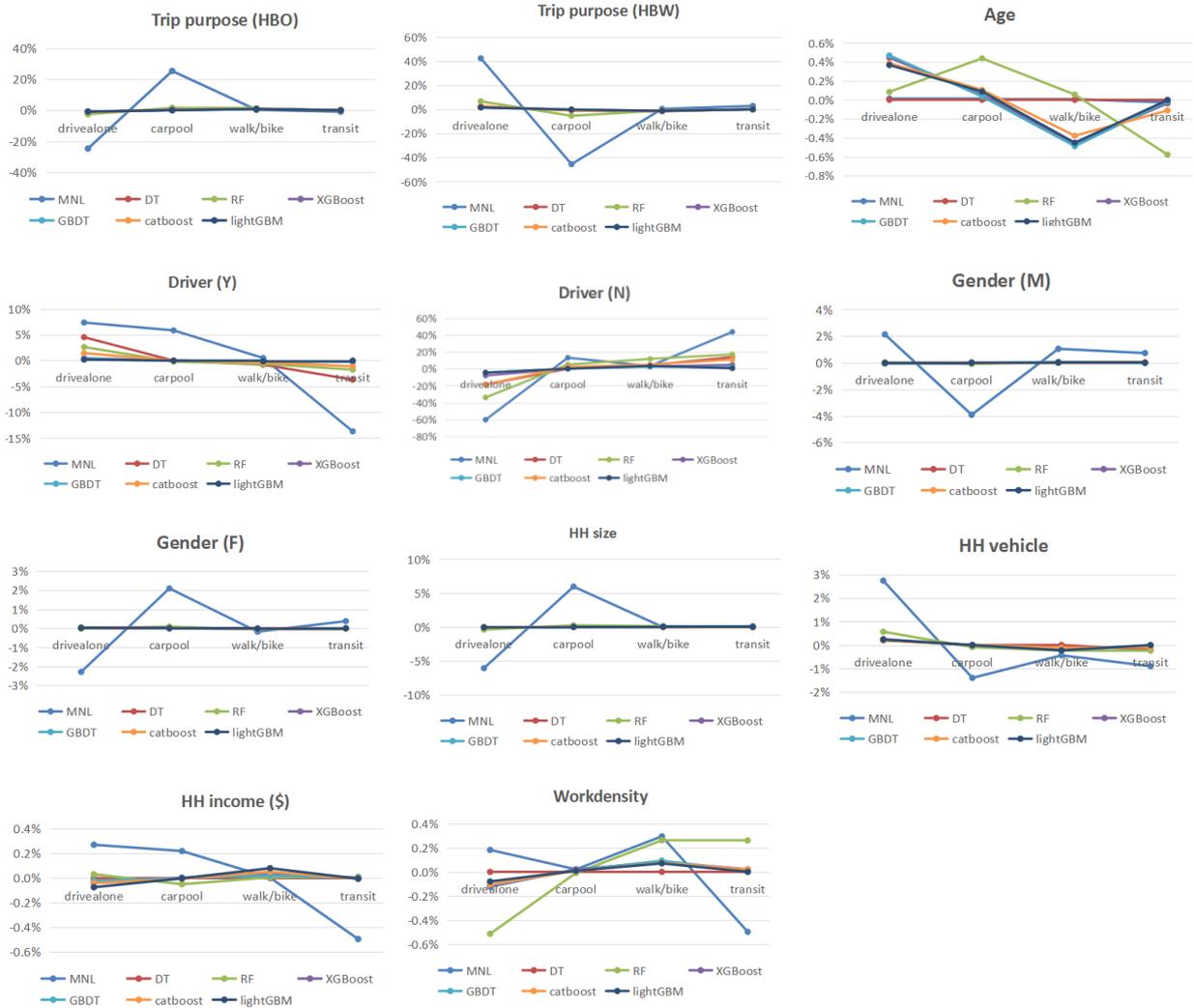
17 (d) Influence of Number of Drivers Increase on HH Vehicle Ownership

18 **Figure 1 VMT & HH Vehicle Ownership Changes: Comparisons of Practical**
 19 **Significance Estimates**

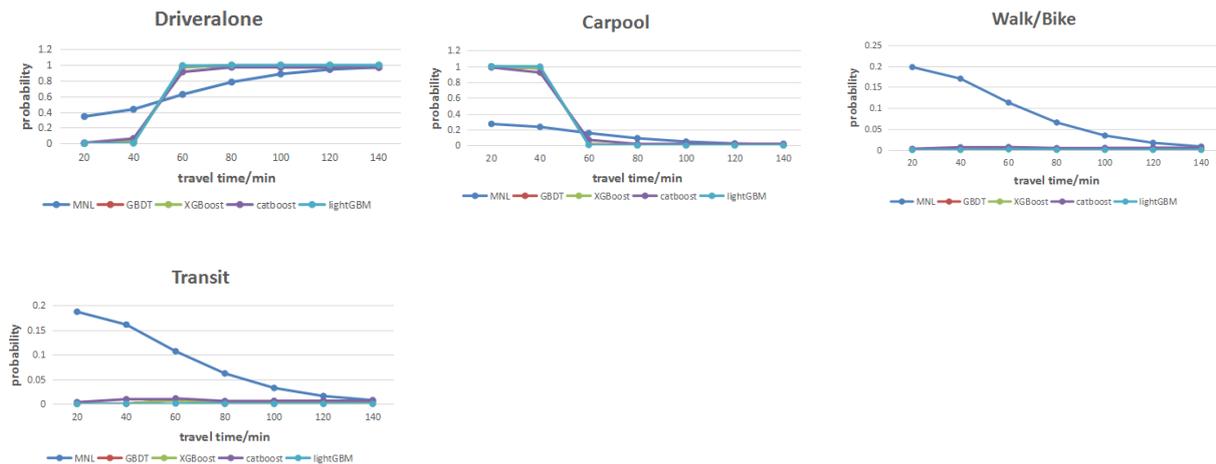


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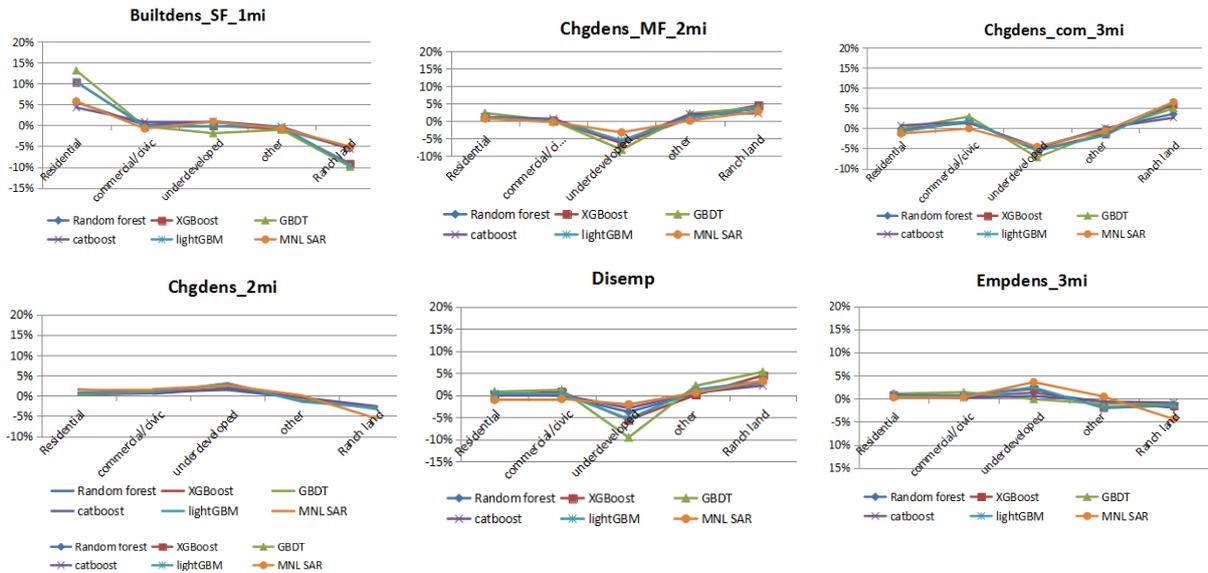
(a) Models Comparison of Influence of Variables on Chosen Probabilities of Each Mode



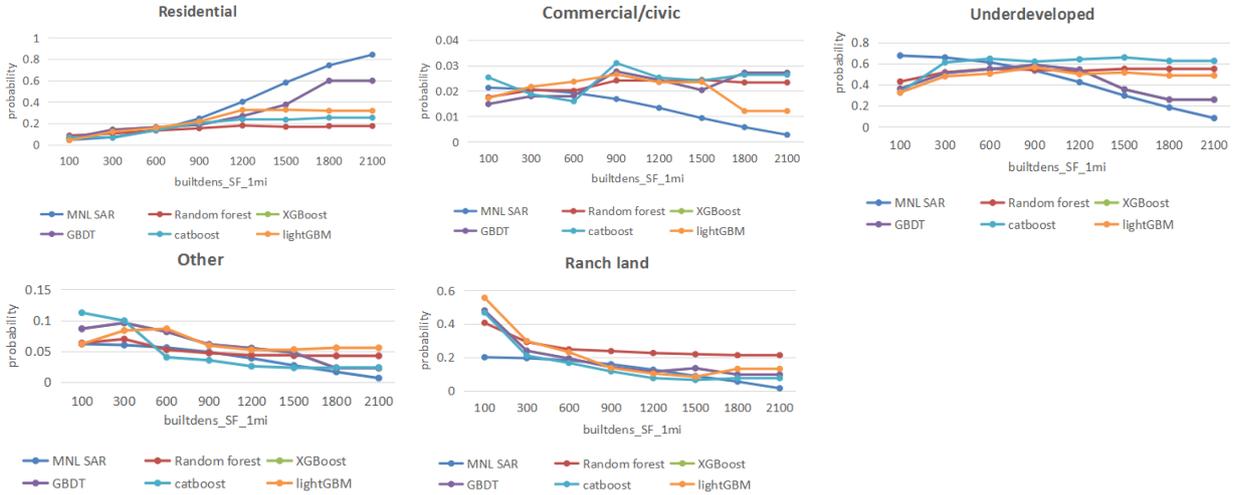
(b) Influence of Travel Time Increase on Chosen Probabilities of Each Mode

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Figure 2 Mode Choice Changes: Comparisons of Practical Significance Estimates



(a) Models Comparison of Influence of Variables on Chosen Probability of Each Land Use Type



(b) Influence of Builtensity of Single Family within 1mi on Land Use Change Probabilities

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2
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Figure 3 Land Use Change: Comparisons of Practical Significance Estimates

4 **Annual HHVMT**

5 As seen in Figure 1 (a), HHSize has a significant impact (around 40%) on HHVMT. The
6 results predicted by the OLS is 1.11 times more than ML models, the practical significance of
7 the number of HH workers is around 2 times more than results of ML methods, and the
8 results of worker density show a huge difference between the OLS and ML methods, while
9 the ML methods share very similar results.

10 As seen in Figure 1 (c), the plot of OLS shows a continuously increase trend, while the ML
11 methods deliver a flattening of response with increase in input values, which is more realistic.
12 Of course, one can add such behaviors to an OLS model, but guessing at additional input
13 variables, but the ML method takes care of this automatically, which is valuable.

14 **HH Vehicle Ownership**

1 As shown in Figure 1 (b), the number of drivers is the most practically significant input used
2 here, followed by home ownership type (rent vs. own). ML and traditional methods are found
3 to deliver very similar estimates of impact for each covariate, apart from the indicator
4 variable “rural”, which is estimated to be 6 times more impactful when using the NegBin
5 model than when using any of the ML methods. As shown in Figure 1 (d), with the increase
6 of numbers of driver in a household, the plot about household vehicle ownership of NegBin
7 model shows a continuously increase trend, while the ML methods deliver a flattening of
8 response with increase in input values, which is more realistic.

9 *Travel Modes*

10 As shown in Figure 2 (a), travel cost and travel time have very sizable impacts on mode
11 choice, in contrast to the effects of trip purpose, traveler gender and HH size. Since the
12 accuracy of the DF, RF, XGBoost, GBDT, and lightGBM models are notably higher than
13 those of the MNL models, the practical significance of the MNL results differ significantly
14 from those generated using ML methods. For example, the Age and Worker density variables
15 show that the ML models prediction results are similar with each other, while the results of
16 the MNL is extremely different from the ML prediction results.

17 The MNL model suggests rather linear relationships between travel time increases and mode
18 choice probabilities. In contrast, the ML methods’ predictions of drive alone and carpool
19 models delivered a sharp decrease or increase, followed by a flattening or plateauing, with
20 little effect on the other two modes’ probability predictions (which stayed around 0%). It is
21 useful to have models that allow for non-monotonic effects, which the ML methods are
22 delivering here, thanks to their behavioral flexibility – without as much mis-prediction as a
23 traditional MNL model can produce. While the ML methods do not offer a random-utility-
24 maximization (RUM) basis for behavior, such functional flexibility is generally realistic and
25 useful to have.

26 *Land Use Changes*

27 The sensitivity tests show how local (1-mile) density of single-family land development has a
28 strong and positive impact on land use change probabilities toward residential land use (as
29 expected), and a negative effect on a shift toward ranchland use. A 2-mile (radius) density of
30 multi-family use built between 1990 and 2010 has a strong negative influence on land use
31 change toward “underdeveloped” status (as per the NCTCOG’s definition of uses).
32 Commercial land use density within 3 miles has a positive influence on land use change
33 toward commercial activities. And distance to an "employment cluster" zip code (in the year
34 2010 data) is found to have a positive influence on ranch land use change.

35 As figure 3 (b) shows, with the increase of build density of single family within 1 mi, the plot
36 of MNL SAR shows an increasing trend, the probability of the pixels’ land use change to
37 residual will be 1 and 0 for other land use type, while the ML methods deliver a flattened or
38 saturated response, as this input rises by 1 SD at a time, the probability of the pixel’ land use
39 change to residual will be about 0.3. Considering the land use aggregation effect, if around of
40 the 30m by 30m pixel are all residential, this pixels’ land use type are more likely to change
41 to residential, so, in the land use change type prediction, the MNL SAR prediction results are
42 more realistic. For the ML, the results of GBDT are more similar to the MNL SAR results,
43 so, the GBDT method not only has a better prediction accuracy but also predict land use
44 change more realistically.

45 Compared to the traditional methods (OLS & MLE) which have own function to show
46 practical significant among X variables and response variable, and add random error terms
47 into their prediction models to consider the uncertainty of Y, learning from the results and
48 analysis above, we can see that some ML methods can always achieve better accuracy no

1 matter for classification or regression problems, and can show the practical significant among
2 X variables and response variable in a more realistic way. By using the ML methods, the
3 prediction model between the X variables and response variable can be obtained after training
4 the data sets, then, new X variables (average of the X variables or increase 1 SD for some
5 variables) can be simulated to seek the quantitative relationship between the X variables and
6 response variable. While it is not wise to only give one predicted Y not consider the
7 uncertainty of the predicted Y, one way to solve this problem is constructing many prediction
8 models, input same X variables into these model and then get the interval of predicted Y.

9 **CONCLUSION**

10 This work explains and applies top ML methods for estimating distinct transportation
11 variables of major interest to planners, policymakers, and the public at large. For example,
12 household vehicle ownership, mode choice and VMT have important consequences for traffic
13 congestion, crash counts, air pollution and energy consumption. Accurate prediction of such
14 variables and understanding of their dependencies on household demographics, land use
15 patterns, transport supply, and policy variables is very valuable. ML makes available a new
16 suite of tools that transportation data analysts can exploit, but we must first understand that
17 weaknesses and strengths, and “open up” the black boxes of the past to appreciate how our
18 choice and attributes impact our final response values. This work demonstrates such
19 applications for a variety of DFW data sets.

20 Based on testing conducted here, using the HHVMT continuous response and vehicle
21 ownership count variables, the GBDT and RF models always performed better than the other
22 ML models, with the RF requiring 13.9 more computing than the GBDT in HHVMT
23 prediction and 30 times more than GBDT in vehicle ownership prediction. The XGBoost,
24 GBDT, catboost and lightGBM all achieved better classification results – for mode choices
25 and land use changes, with the catboost method required the most time for mode choice
26 prediction and lightGBM requiring the least. In land-use change prediction, GBDT required
27 more time. Overall, GBDT was found here to be the best model for the continuous and count
28 response values, while lightGBM is preferred for categorical response prediction.

29 From the practical significance analysis, one finds that methods with similar predictive
30 accuracy deliver similar estimates of each input’s practical significance. For the continuous
31 and count-based response variables (HH VMT and vehicle ownership), output accuracy and
32 input significance are very similar between the traditional and ML methods. In the case of
33 categorical mode choice, the MNL model’s F_1 score was not so competitive, so its estimates
34 of input impact differed from the best-performing methods. In the case of land use change
35 prediction, the ML and SAR-MNL models has similar F_1 score values, and so delivered
36 similar estimates of practical significance across inputs, while the results of SAR-MNL and
37 GBDT are more realistic. But there is less expectation of monotonicity of effect in the ML
38 methods, so an input’s impact can change course or at least flatten, which is valuable in many
39 example cases, as demonstrated in predicting VMT, mode choice and land use change, based
40 on certain input variables.

41 Since ML methods generally outperform traditional statistically-based prediction methods
42 and transportation projects and policies regularly have multi-million-dollar impacts, it is
43 important to at least test such methods to ensure decisions are consistent across modeling
44 assumptions. Planners and modelers have a duty to use limited public resources optimally.
45 Related to this, most policymakers are not concerned about the interpretability of the tools
46 used to reach such conclusions, but many of the best ones are. So it is valuable to try and
47 unpack ML equations, or at least document how outputs vary with respect to each input, for
48 the average observational unit or a sample of such units. Finally, ML methods also remain
49 lacking in terms of conveying uncertainty in predicted output values. For example, is the ML-

1 estimated VMT per year for the average Dallas household 25,320 miles +/- 5200 miles or +/-
2 8400 miles? And what is the probability that this household's oldest adult drives to work
3 rather than bikes to work tomorrow? What software does the data analyst have access to?
4 What programming languages is he/she comfortable with? And how important is immediate
5 transparency in results for application of the model? Or having a behavioral foundation, like
6 random utility maximization for mode choice? These distinctions matter, so important
7 investigative and application work remains for ML users.

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14 The authors confirm contribution to the paper as follows: study conception and design: Li, W.
15 and Kockelman, K.; data collection: Li, W. and Kockelman, K.; analysis and interpretation of
16 results: Li, W. and Kockelman, K.; draft manuscript preparation: Li, W. and Kockelman, K.
17 All authors reviewed the results and approved the final version of the manuscript.

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