**VEHICULAR AD-HOC NETWORK (VANET) SIMULATIONS OF OVERTAKING MANEUVERS ON TWO-LANE RURAL HIGHWAYS**

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**ABSTRACT**

The objective of this paper is to evaluate the effectiveness of a dedicated short-range communication (DSRC)-based wireless vehicle-to-vehicle (V2V) communication system, called the *overtaking assistant*, devised for improving safety during overtaking (also referred to as passing) maneuvers on two-lane rural highways. Specifically, the paper examines the influence of vehicular kinematics (vehicle speeds and accelerations and distances), driver perception-reaction behavior (drivers’ perception/reaction time), and DSRC characteristics (power settings, communication range, packet errors, sensor errors, and estimation inaccuracy) on the effectiveness of DSRC systems in predicting unsafe overtaking maneuvers. To this end, the paper utilizes a microscopic traffic simulator called VEhicles In Network Simulation (VEINS) that supports the simulation of wireless communication protocols in Vehicular Ad-hoc NEtworks (VANETs). Over 13,000 overtaking maneuvers – with over 10,000 collisions and 3,000 safe maneuvers – were simulated to consider heterogeneity in vehicular kinematics, driver behavior, and DSRC performance. The *overtaking assistant* predicts whether a collision will occur and warns the driver before the maneuver begins. A descriptive analysis followed by a multivariate analysis (using binary discrete outcome models) of the simulated data reveals that the majority of collisions that could not be detected were due to the vehicles being out of communication range for the communication power settings used in the simulation. Packet errors, or failed communications, at a rate of up to 50% did not have a significant influence on the ability to detect collisions. These results suggest that the most important step in paving the way toward advanced driver assistance systems for rural highway overtaking maneuvers is to broaden the communication range of DSRC devices. Decreasing packet errors or communication channel congestion beyond the current DSRC standards may not necessarily yield significant benefits for rural highway safety.

**Keywords:** Two-lane rural highways; Overtaking maneuvers; VANETs; Connected vehicles; DSRC driver assistance systems.

**1. INTRODUCTION**

The National Highway Traffic Safety Administration (NHTSA)’s annual crash statistics indicate that two-lane rural highways witness a disproportionately high number of fatal crashes. In particular, although only 19 percent of the US population lives in rural areas, 54 percent of the traffic fatalities occur on rural highways (see FHWA, 2015; NHTSA, 2014). Many of these fatality-causing collisions occur during the passing maneuver on two-lane highways when vehicles attempt to overtake slower moving vehicles ahead. Among the primary reasons behind these collisions are driver errors, including inattention or distraction, misperception of sight distances, illegal passing, and excessive speeds. Despite the implementation of various design solutions and traffic control strategies, such crashes continue to dominate traffic fatality statistics.

Historically, the focus of highway safety has been geared toward implementing passive safety systems (such as airbags and road barriers) that attempt to reduce the severity of crash outcomes. With the advancement of technology, however, efforts have expanded to design advanced driver assistance systems, or ADAS, that attempt to proactively anticipate and prevent crashes. For example, features such as forward collision warning, blind spot detection, lane departure warning, and adaptive cruise control are becoming more prevalent and popular in new vehicle models. However, the development of an *overtaking assistant* – an ADAS that determines whether a gap is considered safe for overtaking, given the trajectory information of the vehicles in the vicinity – has yet to be realized. One particular task of the overtaking maneuver -- determining the location of oncoming traffic (i.e., traffic in the opposite lane) -- is not a task that radars, lasers, or cameras have been able to achieve successfully, mainly because the reported detection ranges of these sensors are shorter than the safe overtaking sight distances (or passing sight distances) recommended in the transportation literature (see Hegeman et al., 2005, Harwood et al., 2008, Delphi, 2009, Velodyne, 2016).

An alternative solution is to use wireless connected vehicle technologies, such as dedicated short-range communication (DSRC) systems, to prevent collisions. Connected vehicle research in the US suggests that 81 percent of all annual crashes can potentially be addressed by vehicle-to-vehicle (V2V) and vehicle-to-infrastructure (V2I) systems (United States Department of Transportation, USDOT, 2015). These technologies rely on wireless communication networks that enable the anticipation of driving situations (i.e., positions, speeds, and acceleration of different vehicles within range of the situation, along with distances between vehicles) at a level of coverage and fidelity that is not feasible with human perception or even with technologies such as radars, cameras, or in-vehicle sensors. Such information can potentially be used to develop accurate collision warning and avoidance systems aimed at assisting overtaking maneuvers.

While wireless communication technologies have the potential to enhance safety during the passing maneuver, most existing studies (see for example Rabadi and Mahmud, 2007; Yang et al., 2011; Joerer et al., 2014b) have focused on the use of these technologies for urban driving situations (such as roadway intersections) and not on overtaking assistance. This paper attempts to fill this gap by undertaking a first assessment of the potential benefits and challenges of using DSRC-based wireless communication systems in the context of overtaking maneuvers on two-lane rural highways. In doing so, the impacts of two broad factors are considered: (a) driver perception-reaction (PR) behavior and vehicular dynamics (speeds and accelerations of different vehicles involved) and (b) DSRC performance. In this paper, DSRC performance refers to the accuracy, efficiency, timeliness and robustness of data transmission among vehicles. The tasks of gathering information (through on-vehicle sensor measurements) to communicate, and of synthesizing communicated information to create a full picture of the present and projected future states of all vehicles, are also considered as dimensions of DSRC performance. Heterogeneity in driver PR time, vehicular dynamics, and DSRC performance that lead to alternate overtaking situations is explicitly accommodated in the analysis.

The paper assesses the potential of wireless communication technologies to assist in overtaking maneuvers using a Vehicular ad-hoc network (VANET) simulator. Such simulators have become the preferred tool for evaluating emerging vehicle safety technologies, offering many advantages over the traditional method of collecting field data. Foremost among these is that it is not feasible to use existing field data when penetration rates for the technologies being assessed are too low or even non-existent (as in our case). VANET simulators, on the other hand, combine a network simulator – with built in network functionality that adheres to DSRC standards for communication among vehicles, as well as between vehicles and infrastructure – with a traffic simulator that allows for flexibility in the design of roadway scenarios and the scalability to support large traffic flows. The specific VANET simulator used here is the VEhIcles in Network Simulator (or VEINS; see Sommer et al., 2011) that supports the simulation of wireless communication protocols in vehicular ad-hoc networks. VANET simulations are run, and the resulting simulated data are analyzed using both descriptive analysis and discrete choice models.

The rest of this paper is structured as follows. The next section outlines related work in the area of overtaking maneuver safety. Section 3 focuses on the design of the collision warning system (called an *overtaking assistant*) simulated in this paper, along with the assumptions made for simulating rural highway overtaking maneuvers (and collisions). Section 4 presents and describes the simulated data, along with a descriptive analysis of the performance indicators of the *overtaking assistant*. Section 5 presents a statistical analysis of the simulated data, using discrete outcome models, and discusses significant findings. Section 6 concludes the paper with recommendations to improve DSRC-enabled driver assistance systems for rural overtaking maneuvers and future research directions.

**2. RELATED WORK**

Overtaking maneuvers are complex cognitive tasks that require the driver to gather and process multiple sources of information and make decisions in short time durations. Hegeman et al. (2005) established a conceptual framework that abstracts the complexity of the overtaking maneuver into 5 different phases – decide to overtake, prepare to overtake, change lane, pass, and return to own lane – which are, in turn, divided into 20 different subtasks. The authors also discussed the feasibility of utilizing ADAS for the 20 different subtasks and mentioned that no ADAS systems existed (then) for complex subtasks such as judging distances with the vehicles in the opposite lane. Many years prior to Hegeman et al., Wilson and Best (1982) categorized different overtaking maneuvers into the following four categories:

1. Normal: The passing vehicle follows the lead vehicle at a constant speed and waits for a sufficient gap to perform an overtaking maneuver. Subsequently, the passing vehicle accelerates to change lane and perform the overtaking maneuver.
2. Flying: The passing vehicle continues at its current speed when initiating the maneuver, no acceleration is involved.
3. Piggy backing: The passing vehicle follows behind another vehicle that is overtaking the lead vehicle.
4. 2+: The passing vehicle performs the overtaking maneuver on two or more vehicles.

Since the introduction of V2V communications, several safety applications have been proposed to reduce the number of accidents caused by unsafe overtaking maneuvers. For example, Olaverri-Monreal et al. (2010) designed an innovative overtaking assistant termed the “See-Through System”. By equipping vehicles with DSRC radios, windshield-installed cameras, and GPS units, the overtaking vehicle was able to send a request to the preceding vehicle to wirelessly send a video stream of its visual perspective. This combination of DSRC, GPS, and video-streaming technology was evaluated using a driving simulator. The communicated video was shown to reduce the time that participants spent behind slower vehicles. All participants who tested this system using the driving simulator reported that the additional information provided would be useful for making overtaking decisions. However, the “See-Through System” was not evaluated with respect to its ability to anticipate and prevent potential collisions. This is possibly because, in the experiments with the “See-Through System”, the decision of whether an overtaking maneuver is safe or not was entirely the driver’s responsibility. We, on the other hand, focus on ADAS that can anticipate potential collisions to help the drivers abort unsafe overtaking maneuvers. To do so, we use a microscopic traffic simulator to simulate a large number of unsafe overtaking maneuvers.

As discussed earlier, microscopic simulators are the preferred method (compared to collecting field data or using driving simulators) for fully evaluating ADAS because of their ability to easily modify individual drivers’ behavior and vehicular characteristics to emulate driver assistance systems. Tapani (2008) developed a Rural Traffic Simulator (RuTSim) with simulation models specific to rural road environments, which Hegeman et al. (2009) used to evaluate an overtaking assistant in terms of safety and traffic congestion. The assistant calculates the time-to-collision with the oncoming vehicle, or the time at which the passing and oncoming vehicles would collide if they were in the same lane, and sends a warning when the time-to-collision is below a threshold value. They showed that an overtaking assistant could significantly increase the safety of overtaking maneuvers without influencing (i.e., decreasing) the average speed of vehicles or the number of successful maneuvers. Another microscopic simulator is the Open Racing Car Simulator (Espie et al., 2008). Wang et al. (2009) used this simulator to estimate the conflict probability of an overtaking vehicle with lead and oncoming traffic by predicting their future positions, using current kinematic information and driver inputs (acceleration, braking, and wheel angle). Several other research studies have also developed their own customized microsimulators to explore different approaches to modeling overtaking behavior (see for example Petrov and Nashashibi, 2011; Ghods and Saccomanno, 2011; Ghaffari et al., 2011; Ghods et al., 2012; Yu et al., 2013). However, all of the above simulators assume that the ADAS has complete and perfect knowledge of all nearby vehicles, without considering potential uncertainties (or errors) in the information obtained and utilized for predicting conflicts or collisions. In fact, most studies mentioned above do not even discuss whether the information is obtained through sensors, V2V communications, or other means. The complete assessment of an ADAS requires a realistic evaluation of its information retrieval method.

Unlike RuTSiM and other microsimulators identified above, VANET simulators have gained traction in the past few years for their ability to evaluate VANET protocols, as well as the potential of connected systems to alleviate traffic congestion and improve traffic safety. VANET simulators couple a traffic simulator with a communications network simulator and turn each vehicle into a wireless node capable of V2V communication. This offers an ability to evaluate the influence of performance issues associated with V2V communications on the effectiveness of ADAS.

In the context of utilizing VANET simulators to assess the effectiveness of ADAS, the main focus in research so far has been on urban intersection scenarios, due to the fact that they are known to be high-incident locations. The few VANET-based studies concerning rural roads have focused mainly on evaluating appropriate communication parameter thresholds to use (such as thresholds in transmission power, beacon rates, and latency) for maximizing throughput and/or minimizing worst-case delays of communication messages, without considering whether the vehicle would end up in a collision or not (see for example Huang et al., 2009; Böhm et al., 2011; Joerer et al., 2014a). However, to determine the effectiveness of safety applications, metrics such as collision probability and number of avoidable collisions need to be captured and validated. Van Kooten (2011) designed communication simulations to study the feasibility of DSRC communication in detecting hazardous overtaking maneuvers, considering failure to communicate before the beginning of a maneuver as failure of the overtaking assistant. We similarly analyze several sources of communication failure, but our performance metrics are defined based on correct detection of potential collisions. In addition, for arriving at the performance metrics, we consider communication failures as well as the possibility of incorrect measurements of vehicle dynamics and incorrect assumptions of driver behavior.

Trajectory prediction algorithms form the basis of collision detection. In reality, even in situations without any communication failures, predicted trajectories may not be completely accurate due to inaccuracies (or errors) in several inputs used in trajectory prediction such as measurement of vehicular dynamics and the assumptions made on driver behavior. Highly inaccurate prediction models can lead to unacceptable rates of undetected collisions or unnecessary warnings, reducing drivers’ trust in the warning system. Vieira et al. (2013) presented a deterministic trajectory prediction method for flying maneuvers and developed a communication strategy to deal with inaccuracies in the prediction. However, the simulations with which they validate their method did not include any error in the trajectory prediction. We study a warning system for normal surface-based overtaking maneuvers (as opposed to flying maneuvers). In addition, we concentrate on how heterogeneity in vehicular dynamics (e.g., speeds, accelerations, and initial distances between vehicles) and inaccuracy in the inputs for trajectory predictions impact overtaking safety.

**3. SIMULATION SETUP**

This section describes the normal overtaking maneuvers simulated on two-lane rural highways, including the definition of unsafe maneuvers (Section 3.1), the characterization of vehicular dynamics in the simulation (Section 3.2), the assumptions made for the DSRC-enabled *overtaking assistant* (Section 3.3), as well as the metrics used for evaluation of the simulated *overtaking assistant* (Section 3.4).

**3.1 Phases of the Overtaking Maneuver and Definition of Unsafe Maneuvers**

Per the terminology of Wilson and Best (1982), we consider a simple, *normal* overtaking maneuver involving three vehicles on a two-lane rural roadway: passing vehicle, lead vehicle, and oncoming vehicle. In Figure 1, the passing, lead, and oncoming vehicles are represented by the white, green, and red colored vehicles, respectively. All three vehicles are considered passenger vehicles, each of length 19 feet.

The simulation is assumed to begin when the passing vehicle indicates its desire to overtake the lead vehicle traveling ahead of it. At the beginning of the simulation (*t* = *t0* = 0), the passing vehicle is assumed to be traveling behind the lead vehicle at a constant speed (i.e., no acceleration, or *ap* = 0 as in Figure 1) in its travel lane; the speed of the passing vehicle is assumed to remain constant for the duration of its driver’s PR time (*tpr*) (as discussed later, we allow this PR time to be heterogeneous in the population of drivers). During the perception/reaction time (0 *≤ t < tpr*), the driver is assumed to perceive and process information on the lead vehicle and oncoming vehicle and determine whether the gap available is safe for completing the overtaking maneuver. At the end of the PR time (*t = tpr*), the passing vehicle is assumed to accelerate and move into the opposite lane. This is considered the start of the overtaking maneuver.

Once in the opposite lane, the passing vehicle is assumed to travel at a constant acceleration *ap* > 0 until it overtakes the lead vehicle and gains a one second *headway* ahead of the lead vehicle. In this context, the term*headway* refers to the time the lead vehicle will require to traverse the gap between the front of the lead vehicle and the back of the passing vehicle (i.e., the time required for the lead vehicle to travel *dl* distance shown in the bottom part of Figure 1). This is equivalent to the time until collision between the lead vehicle and a (hypothetical) stationary object at the rear end position of the passing vehicle in the bottom part of Figure 1. At the time instant that the passing vehicle’s *headway* becomes one second ahead of the lead vehicle, the passing vehicle is assumed to have returned to the original lane to complete the overtaking maneuver, *if* the maneuver were a successful one.

At the moment the passing vehicle’s *headway* becomes one second ahead of the lead vehicle (*t = tfin*), the *time-to-collision* may be calculated between the passing vehicle and the oncoming vehicle. The term *time-to-collision* refers to the amount of time in which the passing vehicle would collide with the oncoming vehicle, had it continued traveling in the opposite lane. To be precise, if the passing and oncoming vehicles maintain their speeds and accelerations at time *t = tfin*, time-to-collision is the time in which the two vehicles would together travel the distance between their front bumpers (denoted by *do* in the last part of Figure 1). If the *time-to-collision* is less than one second, we deem this overtaking maneuver as unsafe, as in Harwood et al. (2008), and label it as resulting in a collision.[[1]](#footnote-1) On the other hand, if the *time-to-collision* is greater than one second, we deem the overtaking maneuver as safe (and resulting in no collision).

Throughout the discussed duration (i.e., from the beginning to the end of the simulation), the lead vehicle and the oncoming vehicle are assumed to travel at their respective constant acceleration rates in their respective lanes, regardless of the position, speed, and acceleration of the passing vehicle.

**3.2 Characterization of Vehicle Dynamics in the Simulation**

Each simulated overtaking maneuver is referred to individually as a *scenario*. Variability (across different overtaking scenarios) in driver behavior and vehicular dynamics can cause overtaking maneuvers to differ from one another. In our simulation, these differences are encapsulated in the following variables: the initial speeds, accelerations, and relative positions of all the three vehicles involved in the maneuver and the perception/reaction time of the passing vehicle’s driver. Each of these variables is drawn randomly for each scenario, with distributional assumptions appropriate to represent realistic variations across different overtaking scenarios, as discussed next.

*3.2.1 Distributions of Simulation Variables*

The passing vehicle’s driver PR time after he/she indicates a desire to overtake is drawn from a triangular distribution between 1 to 4 seconds with a mode of 2.5 seconds. Since PR times vary depending on the driver’s state (e.g., alertness, or fatigue), complexity of the driving situation, and the type of highway (Layton and Dixon, 2012), assuming a maximum of 4 seconds captures that drivers might need longer PR times in rural settings than in urban settings, and in passing maneuvers than in simpler driving tasks.

The initial speeds (i.e., speeds at the beginning of each simulation; denoted by *vp*, *vl*, and *vo* in Figure 1) for the three vehicles are generated from a truncated normal distribution with a mean value 70 mph, minimum value 55 mph, and maximum value 90 mph. Typical speed limits for rural interstates in the US range from 55 to 80 mph (National Motorists Association, 2014). We simulated scenarios over the typical speed limits on rural two-lane highways to capture excessive speeding situations.

The passing vehicle’s acceleration is assumed to be zero at the beginning of the simulation. After the perception/reaction time, the passing vehicle is assumed to accelerate at a constant rate and move into the opposite lane. This acceleration is drawn from a truncated normal distribution with mean 3.6 ft/sec2 and truncated at 1 ft/sec2 and 8.2 ft/sec2 (see Brooks, 2012 for empirical data on accelerations in rural roads). The accelerations for the lead and oncoming vehicles (denoted by *al* and *ao* in Figure 1) are drawn from another normal distribution with mean zero and truncated at 3.2ft/sec2 on both sides of the distribution (Brooks, 2012). Deceleration was allowed only for the lead and oncoming vehicles because the passing vehicle cannot typically overtake (the lead vehicle) while decelerating.

The vehicular dynamics in the simulation begin with positioning the passing vehicle in the right lane at initialization (). Subsequently, the lead vehicle is positioned in the right lane at an arbitrary location (drawn from uniform distribution) ahead of the passing vehicle’s initial location as long as its position is within 15 feet of a one second headway in front of the passing vehicle. The oncoming vehicle’s initial position is set to be uniformly distributed between a lower bound and an upper bound such that the passing and oncoming vehicles are neither too close at the beginning of the overtaking maneuver nor very distant at the end of the maneuver. The lower bound of the allowed distance between the passing and oncoming vehicles was taken as the minimum distance needed for a vehicle (taking the fastest possible maneuver) to successfully overtake, minus one second of headway. In other words, a scenario with an initial passing-oncoming distance at or below the lower bound would never result in a safe maneuver. The upper bound was obtained from the speed-dependent passing sight distance (PSD) guidelines from AASHTO (AASHTO Green Book, 2004).[[2]](#footnote-2) It is worth noting here that the initial vehicle-to-vehicle spacing and other parameters were set such that a considerable proportion of simulated overtaking maneuvers are difficult (but not unrealistic) to complete, since one of the objectives of this research was to assess the usefulness of V2V communications in preventing overtaking crashes. At the same time, certain scenarios were discarded to avoid unrealistic overtaking situations, as discussed next.

*3.2.2 Discarded Scenarios*

Since the focus of this research study is to evaluate DSRC’s effectiveness in an overtaking safety application, some outliers were excluded from the simulated data. Scenarios where the lead vehicle is travelling more than 10 mph faster than the passing vehicle at PR time were discarded, as an overtaking maneuver is very unlikely to occur in such circumstances. Scenarios where the overtaking vehicle failed to pass the lead within 0.621 miles (1 km) were also considered unrealistic and discarded. Finally, scenarios in which the oncoming vehicle passes the lead vehicle before the PR time were discarded.

**3.3 The Simulated DSRC Setup**

In this paper, we simulate a DSRC-enabled *overtaking assistant* that estimates the trajectory of all three vehicles in the above-described overtaking scenario. The purpose of the system is to warn the passing vehicle when it detects a future collision caused by an unsafe overtaking maneuver.

For simulating the *overtaking assistant*, we assume that all vehicles involved have DSRC-enabled V2V communication abilities where each vehicle transmits Cooperative Awareness Messages (CAMs) containing position, speed, and acceleration information every 100 milliseconds. We assume that the *overtaking assistant* requires a switch to be activated to indicate that the passing vehicle would like to overtake the lead vehicle. After this moment (), which is considered the beginning of the scenario, at every 100 milliseconds, the overtaking assistant uses a simple, kinematics-based trajectory prediction model[[3]](#footnote-3) to predict the future positions of the passing vehicle as well as those of the lead and oncoming vehicles within the communication range. Specifically, the *overtaking assistant* extracts vehicle speed and acceleration information (of the lead and oncoming vehicles) and uses this in conjunction with the readings of speed and acceleration from sensors within the passing vehicle itself as inputs into the trajectory prediction model. In this section, we discuss three different parameters of V2V communication effectiveness that have a bearing on the performance of the *overtaking assistant*: (1) Communication range, (2) Packet error rate, and (3) Sensor and estimation errors or inaccuracy.

*3.3.1 Communication Range*

For the *overtaking assistant* to estimate the trajectory of the lead or oncoming vehicles, the two vehicles must be within communication range of the passing vehicle to receive the CAMs containing position, speed, and acceleration information of the lead and oncoming vehicles. The communication range, in turn, depends on the maximum transmit power of the DSRC devices. The Federal Communications Commission defines four classes of DSRC devices depending on their maximum allowed transmit powers as: Class A, Class B, Class C, and Class D. DSRC devices are normally in the Class C category; with a maximum transmit power of 20 decibel-milli Watts (or dBm; dBm is a logarithmic scaled unit of milli Watts) (Kenney, 2011). On the receiving side, devices are only guaranteed to correctly receive messages above a certain power, which is referred to as the minimum sensitivity. IEEE requires the minimum sensitivity of VANET systems to be at least -85 dBm. A wireless signal’s loss in power over distance is measured by its path loss exponent, which has a value of two in free space. We opted to set the path loss exponent to 2.1 due to the low density of vehicles on rural roads. Given these communication strength settings, the communication range in our simulations was approximately 2000 feet. It is worth noting here that Abbas et al. (2012) measured communication range for vehicles on a highway and obtained similar results for these power settings.

The power settings and therefore the range of communication was not varied in our simulations, despite its strong effect on the performance of the collision warning system. This is because its effect is straightforward and deterministic – if an oncoming vehicle is out of communication range when the overtaking begins, there would be no communication of information between vehicles. In such situations, there would be no warning issued by the overtaking assistant, even if the passing maneuver would lead to a collision. Therefore, to ensure timely onset of communications between vehicles involved in overtaking maneuvers, it is useful that the communication range be more than the design-speed dependent safe passing distances given in AASHTO’s Green Book (AASHTO, 2004). At the least, the passing and oncoming vehicles must come within the communication range before the passing vehicle driver’s PR time. Note, however, that increasing the communication range has not been a major focus in the development of DSRC devices since the allocated spectrum is designed to support many other applications (Kenney, 2011); and widely researched applications such as collision warning at intersections or platooning require a much shorter range.

*3.3.2 Packet Error*

When the vehicles are within communication range, the receipt of speed and acceleration information may be affected by communication errors called packet errors that lead to the loss of some CAMs without their receipt. One major cause of these errors is latency, or the delay between a message’s initial broadcast and complete reception. The DSRC standard specifies communication every 100 milliseconds, so a message with latency greater than 100 milliseconds will be abandoned as the next message is sent. Latency is not constant and is determined by many factors, such as congestion caused by high vehicle density. Other miscellaneous issues, including physical interference from precipitation or obstacles and software errors, could also prevent a single message from being received. The term packet error encompasses all these reasons (other than vehicles being outside communication range) why timely communication may not be established between vehicles, and therefore, potential collisions may not be detected by the *overtaking assistant*.

The packet error rate represents the probability of packet error, or the probability that a message sent by one vehicle will not be received by the other vehicles even when the vehicles are within communication range. In our simulations, the following rates of packet error rate were simulated: 0 percent, 50 percent, 75 percent, and 87.5 percent.

*3.3.3 Sensor and Estimation Inaccuracy*

In DSRC enabled connected vehicles, many in-vehicle sensors are used to determine the position, speed, and acceleration of the vehicles. Such sensor measurements are, of course, subject to sensing error (or inaccuracy), which in turn influence the accuracy of the trajectory prediction. To capture this, each simulated measurement of the vehicle position, speed, and accelerations was subject to random noise to represent sensor error (or inaccuracy) of the variables used for trajectory prediction. That is, while the values of the position, speed, and acceleration variables used for simulating each scenario were assumed as “true” values, the corresponding values used for trajectory prediction were subject to sensor error. This is one reason why the trajectory predictions could differ from the simulated trajectories.

The magnitude of sensor error for all variables was controlled by a single noise parameter η. When η is 0 percent, information used for trajectory prediction is assumed to be known perfectly (and same as the simulated values). That is, the values of the vehicle state variables used for trajectory prediction are exactly the same as the simulated values. At 100 percent η, the values used for trajectory prediction are randomly generated (within realistic error bounds) without any regard to the simulated values. For η values between 0 and 100, for a variable *X* with a measurement *x* (i.e., a simulated value *x*), the after-noise measurement , which is used for trajectory prediction, is considered to be uniformly distributed with the following bounds:

In the above equation, *Xrange* is 2 meters for position variables, .5 m/s for speed variables, and .25 m/s2 for acceleration variables. As vehicle positioning is typically achieved by a combination of GPS location and reckoning/filtering, the *Xrange* value position error was taken as half the standard RMS of error for GPS (GPS SPS Performance Analysis Report, 2014). For the velocity and acceleration sensors used within vehicles, the *Xrange* values are chosen such that the sensor error is in the similar range as in standard commercial devices (see Analog Devices Inc., 2009, for an accelerometer example).[[4]](#footnote-4)

In addition to the above discussed sensor errors, it is important to note that the passing vehicle's behavior variables – driver’s PR time and acceleration during overtake – cannot be known with certainty before the beginning of the overtaking maneuver. Therefore, the overtaking assistant has to *estimate* the driver's PR time and acceleration for trajectory prediction purposes. To capture such uncertainty (or errors) in estimation, these two variables were subject to a random noise, using the same control parameter η used for sensor error. The parameters should still follow all previously-outlined assumptions on realistic driving parameters (i.e. the maximum and minimum threshold values assumed in Section 3.2). Thus for a variable *X* with a measurement (or simulated value) *x* and the threshold values , the estimated value is considered to be uniformly distributed with the following bounds:

In our simulations, multiple levels of settings were tested for the sensor/estimation error rate (η) in conjunction with the packet error rate. These are: 0, 50, 75, and 100 percent for the sensor and estimation error parameters (η); and 0, 50, 75, and 87.5 percent for the packet error rate. Between the packet error rate and sensor/estimation error rate, one is kept fixed at the ideal value while the other changes. Specifically, to test the effect of packet error rate, a subset (50 percent) of cases were simulated with the sensor and estimation error parameter (η) set to 0 percent, while changing the packet error rates between values of 0, 50, 75 and 87.5 percent. Similarly, to test the influence of estimation inaccuracy rates, a subset (50 percent) of cases were simulated with the packet error rate set to 0 percent, while changing the sensor/estimation error rate between values of 0, 50, 75 and 100 percent. Note that some of these settings, particularly those with high packet error (higher than 50%) or high sensor inaccuracy rates (higher than 50%) may not be realistic vis-à-vis the current performance of DSRC devices, but are considered in the simulations to allow for worst-case communication settings.

**3.4 Performance Measurement of the Overtaking Assistant**

The purpose of the DSRC-enabled *overtaking assistant* is to detect a future collision (as defined in Section 3.1) due to an unsafe overtaking maneuver and warn the passing vehicle prior to its driver’s PR time. The performance of the *overtaking assistant* may be measured based on how effectively it detects a future collision*.* Specifically, the following two metrics are used to measure the *overtaking assistant’s* performance: (1) *Undetected collisions* and (2) *Unnecessary (or false) warnings*, both of which are defined next.

For the overtaking scenarios that result in a collision (i.e., *time-to-collision* less than a second), an effective *overtaking assistant* must predict the collision (i.e., predicted *time-to-collision* less than a second) and issue a timely warning before the driver’s PR time. Otherwise, the driver will begin to encroach on the oncoming lane and it is assumed to be too late to abort the maneuver. If a scenario results in a collision but a warning is not issued before the driver’s PR time, it is categorized as an *undetected collision*. A collision may go undetected because of two potential reasons: (a) lack of communication between vehicles, or (2) due to errors in the sensing and/or estimation that lead to misprediction of the vehicle trajectories. There are two reasons why communication would not occur between vehicles. First, the vehicles may not be within the communication range. Second, for vehicles within the communication range, packet errors may lead to absence of communication in a timely manner.

*Unnecessary warnings* are issued when communication has been established between all three vehicles, but factors affecting the trajectory prediction model (sensor and estimation inaccuracy) lead to a warning being issued before the driver’s perception/reaction time ends, when in fact, the passing vehicle could have completed the overtaking maneuver safely. In the terminology often used for predictive systems, *undetected collisions* would be considered false negatives and *unnecessary warnings* false positives or false warnings.

In our simulations, the warnings issued do not lead to the passing vehicle aborting the overtaking maneuver. The simulations continue to carry out the maneuver regardless so that we can simulate the outcome of the overtaking maneuver (collision or not), which can be used to determine the accuracy of the issued warnings.

**4. SIMULATED DATA**

The simulated dataset compiled for this research effort includes 13,300 cases, with 10,213 collisions (76.8 percent) and 3,087 (23.2 percent) non-collisions. It is worth noting here that we purposely simulated a higher than realistic proportion of collisions to obtain a sufficient sample of collisions to study.

Of the 10,213 collisions, the DSRC-enabled *overtaking assistant* detected collisions in a timely manner (i.e., detected collision before driver’s perception reaction time) for 7,011 cases (69% successful) but did not detect collisions for the remaining 3,202 cases. Among all the 3,087 simulated successful overtaking maneuvers without a collision, passing vehicles took an average of 9 seconds to complete the overtaking maneuver, which is consistent with the overtaking maneuver times reported in previous literature (Polus et al., 2000; Mocsári, 2009). The *overtaking assistant* detected collisions (i.e., *unnecessary or false warnings*) for less than 3% of the 3,087 successful (or safe) overtaking maneuvers.

Table 1 presents the inputs used across all the overtaking maneuver scenarios studied in this research. These include driver behavior and vehicular dynamics (i.e., PR time, initial speed and acceleration of all the three vehicles – passing, lead, and oncoming vehicles) and V2V communication settings. In addition, initial distances between (1) passing and lead vehicles and (2) passing and oncoming vehicles are presented to give a sense of relative positioning of the vehicles in the beginning of the simulation. As can be observed, the descriptive statistics of the driver behavior and vehicular dynamics parameters are consistent with the assumptions made on these parameters in Section 3.2. The parameters defining V2V communication settings include the frequency of CAM messages, power setting parameters (transmission power, minimum sensitivity, and path loss exponent, packer error rate, and sensor/estimation inaccuracy rates. As discussed in Section 3.3, the frequency of CAM messages and power setting parameters (that result in a certain communication range) were fixed across all simulations, while the packet error rate and sensor and estimation inaccuracy rates were varied.

Comparison of the descriptive statistics between simulated collisions and non-collisions provides insight into how driver behavior and vehicular dynamics might influence collision and non-collision outcomes. Within driver behavior and vehicular dynamics, a higher proportion of passing vehicles with a longer driver PR time ended up in collisions. This result demonstrates the importance of quick and correct decisions in overtaking maneuvers and highlights the need for V2V technologies that can potentially assist in making quick decisions. It can be seen that passing vehicles in the highest speed category (> 80 mph) show a greater chance of avoiding a collision, despite the notion that fast driving is more dangerous. Yet, this result needs to be interpreted with caution, because in our simulations the maximum allowed distances between the passing and oncoming vehicles are speed-dependent (see Section 3.2.1). So fast passing vehicles often start farther away (from oncoming vehicles) than slower vehicles, and therefore might lead to safer simulated maneuvers. Lead vehicles in the slowest speed category (< 70 mph) are also represented in greater proportions in non-collisions than in collisions. A larger proportion of non-collisions started with a larger initial gap between the passing and oncoming vehicles (> 2500ft). A different trend is seen in the case of collisions, where the largest proportion of collision scenarios start with an initial gap of 2000-2500 ft.

One may note that the V2V communication parameters have no influence on simulated collision or non-collision outcomes. This is because the simulations allowed all the overtaking maneuvers to complete despite any warning from the overtaking assistant. Such simulation outcomes are compared with the trajectory prediction outcomes (which depend on the V2V communication settings) to understand the performance of the DSRC enabled overtaking assistant.

Table 2 separates the scenarios into four groups of collision outcomes – undetected collisions, correctly detected collisions, no-collision scenarios without warning, and no-collision scenarios with an unnecessary (or false) warning – to understand the correlation between the performance metrics of the overtaking assistant and the collision outcomes. Note from the third column of the table that V2V communication was established (before PR time of the passing vehicle) between all vehicles for collisions that were detected. As discussed earlier, establishment of communication is necessary for the overtaking assistant to be able to detect potential collisions. On the other hand, note from the second column that V2V communication was not established for a vast majority (98.8%) of collisions that went undetected, suggesting that lack of communication is a major reason why collisions were undetected. Such undetected collisions without V2V communication accounted for a total 3164 scenarios in our simulation. For a vast majority (>97%) of these 3164 undetected collisions where communication was not established, the passing and oncoming vehicles had still not come within communication range (i.e., 2000 feet) before the passing vehicle driver’s PR time. The remaining undetected collisions where the passing and oncoming vehicles were within communication range (constituting only 2.7% of the total undetected collisions) may be attributed to packet errors. All these results suggest that the typical DSRC communication range of 2000 feet may not be sufficient to detect oncoming vehicles in a majority of overtaking scenarios that are prone to collisions.[[5]](#footnote-5)

The last set of rows in Table 2 corresponds to the distribution of the actual time-to-collision - i.e., the time it took for the passing vehicle to collide with the oncoming vehicle after the passing vehicle achieved 1 second headway ahead of the leading vehicle. As expected, the average value of this variable is relatively small in the case of undetected collisions and high in the case of no-collision scenarios. At the same time, between non-collisions without a false warning and non-collisions with a false warning, it may be observed that the time-to-collision is much smaller for the latter scenarios. Specifically, the mean and median values of the time-to-collision variable for no-collision scenarios that were issued a false collision warning are less than 1.5 seconds, suggesting that the majority of scenarios where false warnings were issued were relatively near collisions. Therefore, the issue of false warning does not appear to be a severe issue in the context of DSRC-assisted collision warning systems for overtaking scenarios on rural highways.

Table 3 presents descriptive statistics to understand the influence of packer error and sensor/estimation error rate (or noise) on the performance of the overtaking assistant. The information is presented separately for scenarios that ended up in collisions and scenarios that did not lead to collisions. In each of these two cases (collisions and non-collisions), the percentages across each row add up to 100 percent. For the collisions, the table presents the distribution of the scenarios between undetected collisions and detected collisions for different levels of packer error and sensor and estimation error rates. Similarly, for non-collisions, the table presents the distribution of the scenarios between cases where no warning was issued and cases where a false warning was issued by the overtaking assistant.

As can be observed from the column titled “undetected collisions”, when both packet error rate and noise were set to 0%, 27.4% of the collisions were undetected. All of these undetected collisions may be attributed to lack of communication due to vehicles being out of communication range before the passing vehicles’ PR time. As the packet error increases from 0% to 87.5%, the percentage of collisions that were not detected increases (see the column titled “undetected collisions) whereas the percentage of collisions that were detected decreases (see the column titled detected collisions). However, the increase in the percentage of undetected collisions is small for packet error rates of up to 50%. It is only beyond 50% packet error rates that the percentage of scenarios with undetected collisions increases considerably. In reality, as discussed earlier, packet errors of DSRC devises are rarely as high as 75% or more. Therefore, these results suggest that the influence of packet error rates on missing the detection of a potential collision is not as high as that of the vehicles being out of communication range. Next, note from the non-collisions section of the table that increasing packet error rate did not influence whether or not a false warning is issued for overtaking scenarios that did not end up collisions. This is expected because packet errors influence only whether communication is established or not, not the accuracy of trajectory prediction itself.

The second set of rows correspond to the influence of sensor and estimation error rates (i.e., the noise parameter) on the performance of the overtaking assistant. As can be observed from the collisions section of the table, increasing the sensor and estimation error rate lead to a small decrease in the ability to detect collisions. Specifically, the percentage of collisions that were not detected increase from 27.4% at zero noise to only 28.8% at 100% noise. On the other hand, the percentage of no-collision scenarios that had a false warning issued by the overtaking assistant increase multifold from 0.2% at zero noise to 3.2% at 25% noise and 6.3% at 50% noise. These trends suggest that the sensor and estimation errors are more likely to cause the overtaking assistant to be overly conservative, leading to false warnings, than being overly optimistic, leading to undetected collisions or false negatives. This is expected because the sensor and estimation errors simulated in our experiments were symmetric around the true values (i.e., not biased toward the right or left of the true values) and sensor errors varied with every V2V message sent. Furthermore, only a single prediction of collision is needed at any time between the beginning of the scenario and the PR time of the passing vehicle. While the predicted time-to-collision is equally likely to be conservative or optimistic (because sensor and estimation errors are symmetric), the collision warning is issued on the first instance the predicted time-to-collision is less than 1 second. Therefore, sensor and estimation errors combined with our collision warning protocol primarily increase the likelihood of false warnings. It’s worth noting that symmetric and time-varying noise is likely to have a stronger effect on the overtaking assistant’s performance than constant or one-sided noise, for the same reason: the assistant can overreact to one point in time with exceptional noise.

In summary, the descriptive analysis of the simulated data provides useful insights on the influence of various V2V communication parameters on the effectiveness of DSRC-enabled warning systems in predicting and preventing rural road overtaking collisions. Nevertheless, the univariate descriptive analysis presented here cannot conclusively isolate the influence of different factors on the performance of the DSRC-enabled warning systems. Therefore, the next section provides a multivariate analysis to isolate the influence of each of the above factors while controlling for the influence of vehicular dynamics and driver behavior variables.

**5. MODEL ESTIMATION RESULTS**

The simulated data discussed above were used to estimate three binary discrete outcome models. The first model, called collision occurrence model, was estimated on all 13,300 simulated overtaking maneuvers to examine the influence of driver behavior and vehicular dynamics on collision occurrence (i.e., whether collision occurred or not). The second model, called collision detection model, was on only the subset of simulated overtaking maneuvers that resulted in collisions. This model explores the influence of driver behavior, vehicular dynamics, and V2V communication parameters (packet error rate and sensor/estimation inaccuracy rate) on the ability of the DSRC-enabled *overtaking assistant* to detect collisions[[6]](#footnote-6) in a timely manner (i.e., before the passing vehicle driver’s PR time). The binary outcomes analyzed in this model are: (a) Undetected collision and (b) Detected collision. The third model, called false warning model, was on only the subset of simulated overtaking maneuvers that did not result in collisions. This model was used to examine the influence of various factors on the likelihood of the *overtaking assistant* to provide unnecessary warnings (or false alarm of a collision). The binary outcomes analyzed in this model are: (a) Collision detected but there was no collision (i.e., false warning), and (b) No collision detected and there was no collision. The parameter estimates of all the three models are presented in Table 4.

***Model #1: Collision Occurrence Model***

The collision occurrence model parameter estimates are shown in the second column of the table. The positive coefficient on the passing vehicle driver’s perception/reaction time suggests that higher PR times increased the likelihood of collisions in our simulations. This is because the distance between the passing and oncoming vehicles diminishes as more time elapses from the beginning of the simulation. Also recall that all our simulations continued to complete the overtaking maneuver despite any potential for collisions, because the primary goal of this work is to assess the effectiveness of DSRC-enabled V2V communication systems in predicting and preventing overtaking collisions. In real life situations, however, longer PR times might provide the driver an opportunity for the driver to carefully evaluate the situation and abort the overtaking maneuver if necessary. Similarly, as discussed later, in the context of the DSRC-assisted collision detection systems, longer PR times increase the likelihood of timely detection of collisions.

In the context of the vehicular dynamics of the passing vehicle, *ceteris paribus*, greater initial speeds and higher overtaking accelerations decreased the likelihood of collisions; perhaps because such passing vehicles spend less time in the opposite lane. On the other hand, the initial speed and accelerations of the lead and oncoming vehicles had an opposite influence. Greater speeds and higher accelerations of either vehicle increased the likelihood of collisions. This is because the available gap between passing and oncoming vehicles (when the passing vehicle achieves 1 second headway ahead of the lead vehicle) becomes smaller at higher speeds and accelerations of the lead or oncoming vehicles.

Finally, as expected, smaller initial distance between passing and lead vehicles increased the likelihood of collision, while greater initial distance between passing and oncoming vehicles reduced the likelihood of collision.

***Model #2: Collision Detection Model***

Model #2 may be used to examine the influence of driver behavior, vehicular dynamics and V2V communication settings on the likelihood of a missed warning (or undetected collision) for unsafe overtaking maneuvers. Most of the parameter estimates from this model point to the relative importance of the passing and oncoming vehicles coming within communication range. For instance, in the context of driver behavior, longer PR times of passing vehicle drivers decreased the likelihood of missing the detection of a collision, presumably because longer PR times provide a greater opportunity for the passing and oncoming vehicles to come within communication range.[[7]](#footnote-7) In addition, increasing the speed of oncoming vehicles also increased the likelihood of detecting a collision. More importantly, as can be observed from the high t-statistic values of the variable “initial distance between passing and oncoming vehicles”, this variable exhibits a significant influence on the ability to detect collisions. Specifically, scenarios that began with a greater separation between passing and oncoming vehicles and end in collisions are less likely to be detected in a timely manner. This is again because a greater initial separation between the two vehicles implies a greater likelihood of them not coming within communication range in a timely manner (i.e., prior to passing vehicle’s PR time). All these results suggest that the communication range (of 2000 ft) resulting from the typically-used communication power settings employed in our simulations may not be sufficient to predict and prevent overtaking collisions in a timely manner. This is because, as discussed the previous section, for a majority of unsafe overtaking maneuvers the passing and oncoming vehicles were beyond communication range to be able to detect collisions in a timely manner. These results suggest that increasing the DSRC power settings to broaden the communication range may be an effective way of increasing the performance of DSRC devices for improving the safety of rural highway overtaking maneuvers.

Both the speed and acceleration of the lead vehicle appear to be positively associated with the likelihood of undetected collisions. Increasing the lead vehicle speed increases the amount of time needed for the passing vehicle to complete the overtaking maneuver, thus increasing the likelihood that a distant oncoming vehicle (one outside of communication range) could cause a collision. For the same reason, the acceleration at which the passing vehicle performs the overtaking maneuver is negatively correlated with the likelihood of undetected collisions.

In the context of V2V communication settings, as the packet error rate increased beyond 50 percent, the likelihood of undetected collisions also increased, presumably because it increased the likelihood of missed communication among the three vehicles. However, as discussed earlier, packet error rates of greater than 50% are unlikely in DSRC-enabled V2V communication systems. Therefore, in the context of rural highways where the vehicular traffic volumes are not as high as those in urban environments, relieving communication channel congestion is perhaps not a high-priority concern unless packet error rates increase beyond 50%.

Sensor and estimation errors were not determined to have significant effect on the detection of collisions. Table 3 shows that higher errors will in fact cause slightly fewer collisions to go detected, but this amount is so small as to be probabilistically insignificant according to a multivariate model.

***Model #3: False Warning Model***

The parameter estimates of Model #3 may be used to understand which safe overtaking scenarios are associated with an increased likelihood of an unnecessary warning issued by the overtaking assistant. Specifically, safe overtaking scenarios with lower initial speeds of passing vehicles, higher lead vehicle speeds, or those with higher oncoming vehicle speeds are associated with a higher likelihood of a false warning. This is because passing vehicles with lower initial speeds and lead vehicles with higher speeds tend to require a longer time for completing the overtaking maneuver. Long overtaking maneuvers and fast oncoming vehicles may lead to situations that are near collisions but not collisions (i.e., time-to-collision is higher than 1 second but not by much). This is evident from Table 2, where the median and mean values of time-to-collision variable for no-collision scenarios with a false warning are 1.29 seconds and 1.46 seconds, respectively (see the column titled “Non-collisions with unnecessary warning”). Such overtaking scenarios, although safe, are close to being collisions (i.e., the time-to-collision is slightly greater than 1 second). In such cases, it is perhaps easier for sensor and estimation errors (that influence the trajectory prediction) to cause an under-estimation of the time-to-collision to be below 1 second, leading to a false warning.

In the context of communication settings, as expected, packet error rates do not significantly impact the likelihood of unnecessary warnings. However, increasing the sensor and estimation inaccuracy rates lead to an increase in the likelihood of unnecessary warnings. As discussed at the end of Section 4, this result may be attributed to the unbiasedness of the simulated sensor and estimation errors combined with our protocol to issue a warning at the first instance of predicted time-to-collision falling below 1 second. To reduce such incidence of unnecessary warnings, Haas and Hu (2010) built in logic to their collision warning model to only issue a warning to the driver if the vehicle predicts a collision two consecutive times. However, given the low incidence rate of false warnings (less than 10% at the highest noise setting in our simulations) and that the warnings occurred for scenarios that were near collisions, the issue of false warnings does not appear to be a severe concern for DSRC enabled collision warning systems in rural overtaking settings. Of course, to the extent that sensor and estimation errors in reality might be biased toward being conservative or optimistic, the predictions may also be biased in the same manner.

**6. CONCLUSIONS**

Two-lane rural highways are locations of a disproportionately high number of fatal crashes. A considerable number of these crashes occur during overtaking maneuvers, where vehicles attempt to overtake slower moving vehicles ahead. A potential solution to enhance the safety of rural highways is to utilize connected vehicle technologies such as dedicated short-range communication (DSRC)-enabled collision warning systems to proactively predict and prevent collisions in overtaking scenarios on two-lane highways. However, most existing studies use such connected vehicle technologies in the context of urban driving situations such as urban highway intersections.

The objective of this paper was to assess the effectiveness of a DSRC-enabled collision warning system, called the *overtaking assistant*, devised for detecting unsafe overtaking maneuvers on two-lane rural highways. Specifically, the paper examined the influence of vehicular kinematics (vehicle speeds and accelerations and distances), driver behavior (drivers’ PR time), and DSRC performance characteristics (power settings, communication range, packet errors, sensor errors, and estimation inaccuracy) on the effectiveness of DSRC systems in predicting collisions in overtaking maneuvers. To this end, the paper utilized a microscopic traffic simulator called vehicles in network simulation (Veins) that supports the simulation of wireless communication protocols in vehicular ad-hoc networks (VANETs).

In this study, over 13,000 overtaking maneuvers – with over 10,000 collisions and 3,000 safe maneuvers – were simulated to consider heterogeneity in vehicular kinematics, driver behavior, and DSRC performance. The *overtaking assistant* predicted collisions successfully for 70% of the simulated collisions and gave false collision warnings for less than 3% of simulated safe maneuvers. A descriptive analysis followed by a multivariate analysis (using binary discrete outcome models) of the simulated data reveal that the majority of collisions that could not be detected were due to the passing and lead vehicles being out of communication range (2000ft) when the passing vehicle started the overtaking maneuver (at least for the communication power settings used in the simulation). These results suggest that a promising way forward to enhance the effectiveness of DSRC devices for improving the safety of rural highway overtaking maneuvers is by increasing their power settings to broaden the communication range.

Another notable result is that packet errors below 50% error rate did not have a significant influence on the ability to detect collisions. This result points to how the communication requirements of rural road overtaking scenarios might differ from those of urban intersection scenarios with large traffic volumes where decreasing latency (or packet errors) and relieving communication channel congestion might be a critical need. While still a factor, channel congestion will not have the same magnitude in rural settings as in urban settings. Furthermore, the rural road overtaking maneuver is very deliberate and allows a large span of time in which communication can occur. However, even in rural road settings, latency may be a key factor for other safety applications such as forward collision warning or emergency brake warning.

Sensor error and estimation inaccuracies were found to increase the rate of false warnings more than that of undetected collisions. However, since the incidence of false alarms was small and that a majority of them occurred for scenarios that were near collisions, the issue of false alarms does not appear to be a major concern in the case. It is important to note, however, that any systematic biases in sensor and estimation errors, or systematic errors in the trajectory prediction method, may increase the incidence of false alarms or undetected collisions in ways not covered by this simulation.

This research may be improved in several directions. First, it would be useful to increase the complexity of the simulated overtaking maneuvers to make them more representative of real-life overtaking scenarios. This includes considering the traffic stream beyond the three vehicles we simulated for each overtaking scenario. Second, considering systematic biases in sensor errors and estimation inaccuracies that might occur in real-life collision warning systems will enhance our understanding of the influence of such biases on collision warning systems. Third, the analysis conducted in this study is based on simulated data, with assumptions drawn from the literature and intuition to simulate overtaking maneuvers as realistically as possible. A similar analysis with data collected from the field might help improve the assumptions made to simulate the data. Finally, this paper focuses only on a collision warning system for overtaking maneuvers. While it is useful to study such individual safety systems in isolation, it will become necessary to analyze how the *overtaking assistant* we simulated (or any other advanced driver assistance system) will interact with other increasingly prevalent collision warning systems. For instance, it is important to consider a warning to avoid collision of the passing vehicle with the lead vehicle (i.e., forward collision warning) while also avoiding the collision between the passing and oncoming vehicles.

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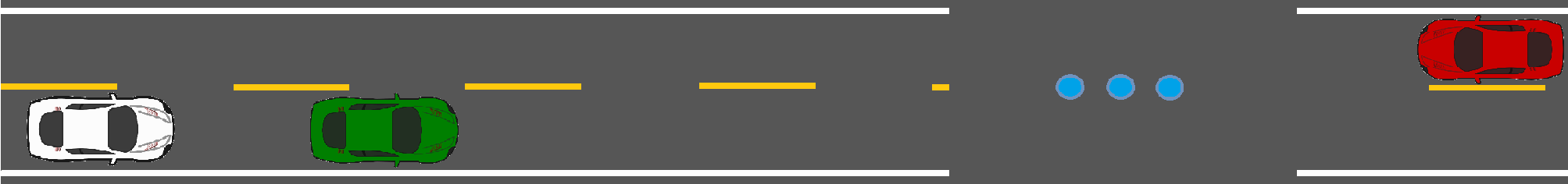
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Oncoming Vehicle

Lead Vehicle

*dl*

Passing Vehicle

*vo*

*vl*

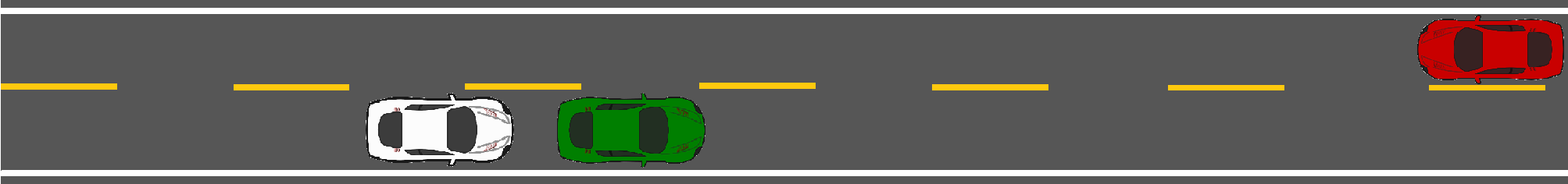
*vp*

*ao*

*al*

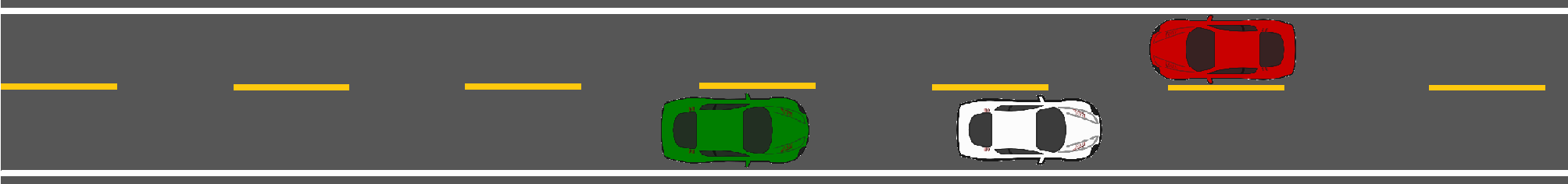
*ap = 0*

*do*



*vp*

*ap*



*dl*

*do*

**Figure 1. Phases of an Overtaking Maneuver**

**Table 1. Descriptive Statistics of the Simulated Data**

|  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
|  | | All Scenarios | Collisions | Non-Collisions |  |  | | All Scenarios | Collisions | Non-Collisions |
| ***No. of observations*** | | 13300 | 10213 | 3087 |  | ***No. of observations*** | | 13300 | 10213 | 3087 |
| **Driver Behavior & Vehicular Dynamics** | | | | | **Driver Behavior & Vehicular Dynamics (continued)** | | | | | |
| **Passing Vehicle** | |  |  |  |  | **Initial Distance between Vehicles** | | | | |
|  | Perception/Reaction Time (Seconds) | | |  |  |  | Passing and Lead (ft) | |  |  |
|  | Min | 1.03 | 1.03 | 1.16 |  |  | Min | 80.6 | 80.6 | 87.6 |
|  | Max | 3.98 | 3.98 | 3.78 |  |  | Max | 166.8 | 166.8 | 161.7 |
|  | <= 3 seconds | 78.4% | 77.6% | 81.0% |  |  | < 120 ft | 29.4% | 35.2% | 10.0% |
|  | > 3 seconds | 21.6% | 22.4% | 19.0% |  |  | 120-140 ft | 46.9% | 46.1% | 49.7% |
|  | Initial Speed (mph) | |  |  |  |  | > 140 ft | 23.7% | 18.6% | 40.4% |
|  | Min | 46.96 | 46.96 | 56.87 |  |  | Passing and Oncoming (ft) | |  |  |
|  | Max | 89.95 | 89.81 | 89.95 |  |  | Min | 1351 | 1351 | 1649 |
|  | < 70 mph | 30.8% | 37.8% | 7.5% |  |  | Max | 3771 | 3723 | 3771 |
|  | 70-80 mph | 40.5% | 41.2% | 38.3% |  |  | < 2000 ft | 19.7% | 23.6% | 7.0% |
|  | > 80 mph | 28.7% | 21.0% | 54.2% |  |  | 2000-2500 ft | 43.7% | 48.3% | 28.3% |
|  | Overtaking Acceleration (ft/s²) | | |  |  |  | > 2500 ft | 36.6% | 28.1% | 64.6% |
|  | Min | 1.01 | 1.18 | 1.01 | **V2V Communication Settings** | | | | | |
|  | Max | 8.20 | 8.20 | 8.19 |  | **Frequency of Cooperative Awareness Messages** | | | | |
|  | < 3 ft/s² | 28.9% | 31.5% | 20.4% |  |  | 100 ms | 100% | 100% | 100% |
|  | 3-5 ft/s² | 46.3% | 46.5% | 45.4% |  | **Transmission Power** | | |  |  |
|  | > 5 ft/s² | 24.8% | 21.9% | 34.2% |  |  | 20 dBm | 100% | 100% | 100% |
| **Lead Vehicle** | |  |  |  |  | **Minimum Sensitivity** | | |  |  |
|  | Speed (mph) |  |  |  |  |  | -85 dBm | 100% | 100% | 100% |
|  | Min | 55.01 | 55.01 | 55.02 |  | **Path Loss Exponent** | | |  |  |
|  | Max | 89.98 | 89.98 | 89.33 |  |  | 2.1 | 100% | 100% | 100% |
|  | < 70 mph | 49.2% | 43.3% | 68.5% |  | **Packet Error Rate** | | |  |  |
|  | 70-80 mph | 37.3% | 40.8% | 25.6% |  |  | 0% | 57.1% | 57.1% | 57.1% |
|  | > 80 mph | 13.5% | 18.0% | 5.9% |  |  | 50% | 14.3% | 14.3% | 14.3% |
|  | Acceleration (ft/s²) | |  |  |  |  | 75% | 14.3% | 14.3% | 14.3% |
|  | Min | -3.18 | -2.92 | -3.18 |  |  | 87.5% | 14.3% | 14.3% | 14.3% |
|  | Max | 3.10 | 3.10 | 2.56 |  | **Sensor and Estimation Inaccuracy Rate (or Noise)** | | |  |  |
|  | <= 0 ft/s² | 52.4% | 47.8% | 67.6% |  |  | 0% | 57.1% | 57.1% | 57.1% |
|  | > 0 ft/s² | 47.6% | 52.2% | 32.4% |  |  | 25% | 14.3% | 14.3% | 14.3% |
| **Oncoming Vehicle** | | |  |  |  |  | 50% | 14.3% | 14.3% | 14.3% |
|  | Speed (mph) |  |  |  |  |  | 100% | 14.3% | 14.3% | 14.3% |
|  | Min | 55.00 | 55.03 | 55.00 |  |  |  |  |  |  |
|  | Max | 89.97 | 89.97 | 89.83 |  |  |  |  |  |  |
|  | < 70 mph | 50.4% | 48.7% | 56.0% |  |  |  |  |  |  |
|  | 70-80 mph | 36.6% | 37.9% | 32.2% |  |  |  |  |  |  |
|  | > 80 mph | 13.0% | 13.4% | 11.8% |  |  |  |  |  |  |
|  | Acceleration (ft/s²) | |  |  |  |  |  |  |  |  |
|  | Min | -3.24 | -2.85 | -3.24 |  |  |  |  |  |  |
|  | Max | 3.19 | 3.19 | 2.78 |  |  |  |  |  |  |
|  | <= 0 ft/s² | 50.0% | 48.7% | 54.4% |  |  |  |  |  |  |
|  | > 0 ft/s² | 50.0% | 51.3% | 45.6% |  |  |  |  |  |  |

**Table 2. Performance Assessment of the DSRC-enabled V2V Communication System**

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
|  | **Undetected Collisions** | **Detected Collisions** | **Non-collisions without any false warning** | **Non-collisions with unnecessary warning** | **All Scenarios** |
| ***No. of observations*** | 3202 | 7011 | 3005 | 82 | 13300 |
| **V2V Communication established before perception/reaction time** |  |  |  |  |  |
| Yes | 1.2% | 100% | 30.0% | 100% | 60.4% |
| No | 98.8% | 0% | 70.0% | 0% | 39.6% |
| **Passing and oncoming vehicles within communication range before perception/reaction time** |  |  |  |  |  |
| Yes | 2.7% | 100% | 32.4% | 100% | 61.3% |
| No | 97.3% | 0% | 67.6% | 0% | 38.7% |
| **Warning timestamp (seconds)** |  |  |  |  |  |
| Min | -- | 0.100 | -- | 0.100 | 0.100 |
| Max | -- | 3.800 | -- | 3.100 | 3.800 |
| Mean | -- | 1.025 | -- | 1.141 | 1.026 |
| Std. Dev. | -- | 0.875 | -- | 0.804 | 0.874 |
| **Actual time-to-collision (seconds)** |  |  |  |  |  |
| 0 seconds | 85.4% | 91.7% | 0% | 0% | 68.9% |
| Min | 0.000 | 0.000 | 1.005 | 1.005 | 0.000 |
| Max | 0.997 | 0.997 | 8.864 | 4.584 | 8.864 |
| Median | 0.000 | 0.000 | 2.774 | 1.286 | 0.000 |
| Mean | 0.077 | 0.388 | 3.158 | 1.461 | 0.946 |
| Std. Dev. | 0.215 | 0.154 | 1.616 | 0.516 | 0.784 |

**Table 3. Overtaking Assistant Accuracy Measures**

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
|  | **Collisions** | | **Non-collisions** | |
|  | **Undetected Collisions** | **Detected Collisions** | **No Warning** | **False Warning** |
| **Packet Error Rate** (while keeping sensor & estimation error at 0%) | | | | |
| 0% | 27.4% | 72.6% | 99.8% | 0.2% |
| 50% | 29.7% | 70.3% | 99.8% | 0.2% |
| 75% | 33.7% | 66.3% | 99.8% | 0.2% |
| 87.50% | 43.8% | 56.2% | 99.8% | 0.2% |
| **Sensor & Estimation Error Rate** **or Noise** (while keeping packet error at 0%) | | | | |
| 0% | 27.4% | 72.6% | 99.8% | 0.2% |
| 25% | 27.9% | 72.1% | 96.8% | 3.2% |
| 50% | 28.1% | 71.9% | 93.6% | 6.3% |
| 100% | 28.8% | 71.1% | 91.8% | 8.1% |

**Table 4. Binary Probit Model Estimation Results**

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
|  |  | **Model #1** | **Model #2** | **Model #3** |
|  |  | Collision Occurrence  (base: Non-Collisions) | Undetected Collisions  (base: Collision occurred and warning issued) | False Warnings  (base: No collision and warning not issued) |
| ***No. of observations*** | | 13300 simulated overtaking maneuvers | 10213 simulated overtaking maneuvers that lead to collisions | 3187 simulated overtaking maneuvers that did not lead to collisions |
|  | | Coefficient (t-stat) | Coefficient (t-stat) | Coefficient (t-stat) |
| ***Constant*** | | -0.2938 (-6.07) | -0.9916 (-22.23) | -4.5701 (-11.95) |
| ***Passing Vehicle*** | |  |  |  |
|  | Perception/Reaction Time |  |  |  |
|  | <= 3 seconds | base category | base category | base category |
|  | > 3 seconds | 0.2903 (6.87) | -1.4238 (-26.67) | -- |
|  | Initial Speed |  |  |  |
|  | < 70 mph | 0.9332 (16.66) | -- | 0.4590 (2.29) |
|  | 70-80 mph | base category | base category | -- |
|  | > 80 mph | -1.2391 (-25.41) | -- | base category |
|  | Overtaking Acceleration |  |  |  |
|  | < 3 ft/sec2 | 0.5527 (13.01) | 0.2415 (6.04) | -- |
|  | 3-5 ft/sec2 | base category | base category | base category |
|  | > 5 ft/sec2 | -0.5295 (-13.16) | -- | -- |
| ***Lead Vehicle*** | |  |  |  |
|  | Speed |  |  |  |
|  | < 70 mph | base category | base category | base category |
|  | 70-80 mph | 2.0358 (37.50) | -- | 0.416 (1.94) |
|  | > 80 mph | 3.2613 (37.66) | 0.3063 (6.11) | 0.416 (1.94) |
|  | Acceleration |  |  |  |
|  | <= 0 ft/s² | base category | -0.1253 (-3.39) | base category |
|  | > 0 ft/s² | 1.0309 (27.07) | base category | -- |
| ***Oncoming Vehicle*** | |  |  |  |
|  | Speed |  |  |  |
|  | < 70 mph | base category | base category | base category |
|  | 70-80 mph | 0.5316 (14.27) | -0.1365 (-3.67) | 0.3809 (2.56) |
|  | > 80 mph | 0.6033 (10.81) | -0.1365 (-3.67) | 0.3809 (2.56) |
|  | Acceleration |  |  |  |
|  | <= 0 ft/s² | -0.3286 (-9.70) | -- | base category |
|  | > 0 ft/s² | base category | base category | -- |
| ***Initial Distance between Vehicles*** | |  |  |  |
|  | Passing and Lead |  |  |  |
|  | < 120ft | 0.2623 (4.86) | -0.2272 (-5.40) | -- |
|  | 120-140 ft | base category | base category | base category |
|  | > 140 ft | -- | -- | -- |
|  | Passing and Oncoming |  |  |  |
|  | < 2000 ft | 0.8437 (15.84) | -1.1740 (-15.08) | 1.9539 (7.79) |
|  | 2000-2500 ft | base category | base category | 1.6197 (8.60) |
|  | > 2500 ft | -1.2493 (-26.89) | 2.4599 (48.57) | base category |
| ***V2V Communication Settings*** | |  |  |  |
|  | Packet Error Rate |  |  |  |
|  | 0% | \*\* | base category | base category |
|  | 50% | \*\* | -- | -- |
|  | 75% | \*\* | 0.3317 (5.65) | -- |
|  | 87.5% | \*\* | 0.9038 (17.08) | -- |
|  | Sensor & Estimation Error Rate |  |  |  |
|  | 0% | \*\* | base category | base category |
|  | 25% | \*\* | -- | 1.2327 (3.87) |
|  | 50% | \*\* | -- | 1.6477 (5.52) |
|  | 100% | \*\* | -- | 1.7781 (5.93) |
| **Summary Statistics** | |  |  |  |
|  | No. of observations: | 13300 | 10213 | 3087 |
|  | R2 | 0.48 | 0.51 | 0.36 |
|  | Restricted Log-Likelihood: | -7203.52 | -6350.23 | -378.337 |
|  | Final Log-Likelihood: | -3709.41 | -2978.21 | -241.748 |
| \*\* Not included in model. V2V communication only warns of a potential collision but does not influence the simulated outcome. | | | | |
| -- Dropped from specification as the coefficient was statistically insignificant (i.e., not different from zero). | | | | |

1. Of course, not all situations where the *time-to-collision* is less than one second may result in collisions. To be precise, a collision happens only when the time gap goes to zero or beyond. However, since it is not safe to be within such a small *time-to-collisio*n we deem all such collision-prone situations (with less than one second *time-to-collision*) as collisions. [↑](#footnote-ref-1)
2. The PSD calculations from the AASHTO Green Book are used to set the upper bound on the initial distance between the passing vehicle and the oncoming vehicles, because these PSD values are considered to be very conservative in the literature (Harwood et al., 2008). [↑](#footnote-ref-2)
3. The details of the trajectory prediction model are not provided here, since the model is based on simple kinematics involving the three vehicles. Interested readers may contact the authors for details. [↑](#footnote-ref-3)
4. The error bounds on each variable are relative to its assumed possible error, not the overall range or significance of its values. A separate study with a different variable to represent error on each of the eight sensed variables is outside the scope of this paper. [↑](#footnote-ref-4)
5. As discussed earlier, the typically used DSRC power settings employed in our simulations imply a communication range of about 2000 feet. However, this doesn’t necessarily imply that V2V communication is fully present before 2000 feet and becomes completely absent right after 2000 feet. Rather, the strength of the communication is likely to taper continuously (but quickly) beyond 2000 feet. [↑](#footnote-ref-5)
6. Recall that a collision would be detected if the estimated *time-to-collision* (i.e., time to collision at the instance passing vehicle’s headway is 1 second ahead of the lead vehicle) is less than 1 second. [↑](#footnote-ref-6)
7. Longer PR times also result in a higher likelihood for the V2V communication to overcome packet loss, which in turn, increases the likelihood of detecting collisions. [↑](#footnote-ref-7)